

YAKUBOVICH, V. A.

SOV/2660

PHASE I BOOK EXPLOITATION

16(1) Vesoyuznyy matematicheskiy s'yezd. 3rd, Moscow, 1956  
Trudy. t. 1. Raznyye otdelnyye sektsionnyye doklady. Doklady Inostrannykh uchennykh (Transactions of the 3rd All-Union Mathematical Conference in Moscow, vol. 1. Summary of Section Reports. Reports of Foreign Scientists) Moscow, Izd-vo AN SSSR, 1959. 247 p. 2,200 copies printed.

Sponsoring Agency: Akademiya nauk SSSR. Matematicheskiy institut. Tech. Ed.: G.M. Shevchenko; Editorial Board: A.A. Abramov, V.G. Izrael'skiy, A.M. Vasiliyev, B.V. Medvedev, A.D. Ryankis, S.M. Nikol'skiy (Resp. Ed.); A.G. Postnikov, Yu. V. Prokhorov, E.A. Rabinov, P. L. Ul'yanskiy, V.A. Uspenskiy, M.O. Chetayev, G. Ye. Shilov, and A.I. Shirshov.

PURPOSE: This book is intended for mathematicians and physicists. COVERAGE: The book is Volume IV of the Transactions of the Third All-Union Mathematical Conference, held in June and July 1956. The book is divided into two main parts. The first part contains summaries of the papers presented in the first two volumes. The second part contains the text of reports submitted to the editor by non-Soviet scientists. In those cases when the editor, the title list did not submit a copy of his paper to be printed in a previous volume, reference is made to the appropriate volume. The papers, both Soviet and non-Soviet, cover variational, function theory, algebra, differential and integral equations, topology, mathematical problems of mechanics and physics, computational mathematics, functional logic and the foundations of mathematics, and the history of mathematics.

Shirshov, A.I. (Moscow). On the problem of the boundedness of solutions of a system of linear differential equations with periodic coefficients	37
Dumarkin, S.I. (Moscow). Asymptotic solution of linear non-homogeneous differential equations and its applications to the design of shells and blades	39
Chernik, V.A. (Voronezh). Singular differential equations	40
El'sgolts, L.E. (Moscow). Periodic solutions of quasilinear differential equations with delayed argument	41
Yakubovich, V.A. (Leningrad). Extension of certain studies of the theory of a differential equation of the second order to anomalous systems with periodic coefficients	41
Yezhov, E.E. (Moscow). On discontinuities in solutions of quasilinear equations	42

YAKUBOVICH, V. A.: Doc Phys-Math Sci (diss) -- "A system of linear differential equations in canonic form with periodic coefficients". Leningrad, 1959. 21 pp (Leningrad Order of Lenin State U im A. A. Zhdanov), 150 copies (KL, No 14, 1959, 117)

YAKUBOVICH, V.A. (Leningrad)

Small-parameter method for canonical systems with periodic coefficients. Prikl. mat. i mekh. 23 no.1:15-34 Ja-F '59. (MIRA 12:2)

(Differential equations)

16(1)

AUTHOR:

Yakubovich, V.A.

SOV/20-124-3-10/67

TITLE:

Oscillation Properties of the Solutions of Linear Canonical Systems of Differential Equations (Otsillyatsionnyye svoystva resheniy lineynykh kanonicheskikh sistem differentsial'nykh uravneniy)

PERIODICAL:

Doklady Akademii nauk SSSR, 1959, Vol 124, Nr 3,  
pp 533-536 (USSR)

ABSTRACT:

The author considers the system

$\frac{dx}{dt} = JH(t)x$ , where  $x$  is a  
2k-dimensional vector,

$$H(t) = \begin{pmatrix} \alpha & \beta \\ \beta^* & \gamma \end{pmatrix}, \quad \alpha = \alpha^t, \quad \gamma = \gamma^t,$$

$J = \begin{pmatrix} 0 & I_k \\ -I_k & 0 \end{pmatrix}$ ,  $I_k$  unit matrix,  $H(t) = H(t)^*$  a real symmetric matrix. The author uses results of I.M. Gel'fand, V.B. Lidskiy, I.M. Glazman, L.D. Nikolenko etc, in order to formulate seven theorems after having introduced many definitions; these theorems overlap with well-known results of Sternberg [Ref 5]

Card 1/2

Oscillation Properties of the Solutions of Linear  
Canonical Systems of Differential Equations

SOV/20-124-3-10/67

and others or, however, already implicitly occur in other investigations.

There are 10 references, 7 of which are Soviet, 2 American, and 1 Portuguese.

ASSOCIATION: Nauchno-issledovatel'skiy institut matematiki i mekhaniki  
Leningradskogo gosudarstvennogo universiteta imeni A.A.Zhdanova  
(Scientific Research Institute for Mathematics and Mechanics  
of the Leningrad State University imeni A.A. Zhdanov)

PRESENTED: September 22, 1958, by V.I. Smirnov, Academician

SUBMITTED: September 15, 1958

Card 2/2

16(1)

AUTHOR:

Yakubovich, V.A.

SOV/20-124-5-9/6:

TITLE:

Conditions for the Oscillation and Nonoscillation for Linear Canonical Systems of Differential Equations (Usloviya kolebatel'nosti i nekolebatel'nosti dlya lineynykh kanonicheskikh sistem differentsial'nykh uravneniy)

PERIODICAL: Doklady Akademii nauk SSSR, 1959, Vol. 124, Nr. 5, pp. 994-997 (USSR)

ABSTRACT: The author considers the system

$$(1) \quad \frac{dx}{dt} = JH(t)x,$$

where  $x$  is a  $2k$ -dimensional vector,  $H(t) = \begin{pmatrix} \alpha & \beta \\ \beta^* & \gamma \end{pmatrix}$ ,  $\alpha = \alpha^*$ ,  $\gamma = \gamma^*$ ,

$J = \begin{pmatrix} 0 & I_k \\ -I_k & 0 \end{pmatrix}$ ,  $H(t) = H(t^*)$  real symmetric  $2k \times 2k$  matrix. Let  $x_1, \dots$

$\dots, x_k$  be linearly independent solutions of (1), where it is

$(Jx_j, x_h) = 0$ . Let  $\begin{pmatrix} U \\ V \end{pmatrix}$  be a  $k \times 2k$  matrix, the columns of which are the vectors  $x_1, \dots, x_k$ . Let  $X(t)$  be the matricant of (1),

see [Ref 1];  $\text{Arg } X(t) = \text{Arg det } [U(t) - iV(t)]$ . The equation (1) is called oscillating, if  $\text{Arg } X(t)$  for  $t \rightarrow \infty$  is not bounded;

Card 1/2

Conditions for the Oscillation and Nonoscillation for SOV/20-124-5-9/62  
Linear Canonical Systems of Differential Equations

(1) is called nonoscillating, if  $\text{Arg } X(t)$  is bounded. In eight theorems the author gives several conditions for the oscillation and nonoscillation in the above sense, e.g.:

Theorem: If starting from  $t_0 > 0$  it is almost everywhere

$\Delta < 0$ ,  $\delta \neq 0$  (or conversely), then (1) is nonoscillating.

The results overlap or generalize the results of I.M.Glazman, V.A.Kondrat'yev, L.D.Nikolenko.

There are 7 references, 5 of which are Soviet, and 2 American.

ASSOCIATION: Nauchno-issledovatel'skiy institut matematiki i mekhaniki  
Leningradskogo gosudarstvennogo universiteta imeni A.A.  
Zhdanova (Scientific Research Institute of Mathematics and  
Mechanics of the Leningrad State University imeni A.A.Zhdanov)

PRESENTED: September 22, 1958, by V.I.Smirnov, Academician

SUBMITTED: September 15, 1958

Card 2/2

69757

S/043/60/000/C2/08/011

10.9500 16.3400

AUTHOR: Yakubovich, V.A.

TITLE: On Nonlinear Differential Equations of Automatic Control Systems  
With One Control Unit

PERIODICAL: Vestnik Leningradskogo universiteta, Seriya matematiki,  
mekhaniki i astronomii, 1960, No.2, pp 120-153

TEXT: This is a detailed representation of the results on the method of  
A.I.Lur'ye (Ref.1) announced by the author in (Ref.4,5). There are  
overlappings with the books of A.M.Letov (Ref.2) and P.V.Bromberg (Ref.3).  
The author mentions V.M.Popov, V.A.Plass, Ayzurma., Professor D.K.Faddeyev,  
A.B.Konstantinova, Ye.A.Barbashin and N.N.Krasovskiy.  
There is 1 figure and 17 references: 15 Soviet and 2 German.

Card 1/1



YAKUBOVICH, V.A.

Nonlinear differential equations of automatic control systems  
with one regulating element. Vest.LGU 15 no.7:120-153  
'60. (MIRA 13:4)  
(Automatic control) (Differential equations)

S/043/60/000/13/09/016  
C111/C222

AUTHOR: Yakubovich, V.A.

TITLE: On Radius of Convergence of Series in the Small Parameter Method  
for the Linear Differential Equations With Periodic Coefficients

PERIODICAL: Vestnik Leningradskogo universiteta, Seriya matematiki,  
mekhaniki i astronomii, 1960, No. 13, pp. 81 - 89

TEXT: If the solution of a linear system of differential equations with periodic coefficients is sought in the form  $X(t, \epsilon) = P(t, \epsilon)e^{K(\epsilon)t}$ , where the matrix  $K(\epsilon)$  and the periodic matrix  $P(t, \epsilon)$  are series in  $\epsilon$ , where  $K(\epsilon) = \ln X(1, \epsilon)$ , then in general there can appear different radii of convergence for  $K(\epsilon)$  because of the nonuniqueness of the logarithm. The author proves a theorem which is partially known (compare (Ref. 10)) which together with some qualitative considerations permits to make the calculations in the above mentioned method so that there results the greatest radius of convergence.

Card 1/2

On Radius of Convergence of Series in the  
Small Parameter Method for the Linear  
Differential Equations With Periodic Coefficients

S/043/60/000/13/09/016  
C111/C222

The author mentions N.N. Bogolyubov, Yu.A. Mitropol'skiy, N.A. Artem'yev,  
I.Z. Shtokalo, N.P. Yerugin, and M.G. Kreyn.  
There are 2 figures and 13 references : 12 Soviet and 1 Italian.

Card 2/2

✓

16.6800 (1024, 1250, 1344)  
16,3400

84655

S/020/60/135/001/006/030  
C111/C222

AUTHOR: Yakubovich, V.A.

TITLE: Stability<sup>b</sup> Conditions in the Large for Some Non-Linear  
Differential Equations of Automatic Control

PERIODICAL: Doklady Akademii nauk SSSR, 1960, Vol. 135, No. 1, pp 26-29

TEXT: The author considers the system

$$(1) \quad \frac{dx}{dt} = Ax + a\varphi(\sigma), \quad \frac{d\sigma}{dt} = (b, x) - \rho\varphi(\sigma),$$

where  $x$ ,  $a$  and  $b$  are vectors,  $A$  - matrix,  $(b, x)$  - scalar product and  $\varphi(\sigma)$

is a real continuous function;  $\rho > 0$ ;  $0 < \mu_1 \leq \frac{\varphi(\sigma)}{\sigma} \leq \mu_2 < +\infty$  ( $\sigma \neq 0$ ).

Furthermore it is assumed that the eigenvalues of the matrix

$$(2) \quad K = \frac{1}{\rho} (A^* + \frac{1}{\rho} ba^*)$$

lie in the left halfplane. For an arbitrary matrix  $H$  let  $H > 0$  mean that  $H$  is  
Card 1/ 5

84655

Stability Conditions in the Large for Some  
Non-Linear Differential Equations of  
Automatic Control

S/020/60/135/001/006/030  
C111/C222

symmetric and positive definite.

Theorem 1: Take an arbitrary matrix  $G_0 > 0$  and define the matrices  $H_0 > 0$ ,  $M(\sigma)$  and the vectors  $a_0$  and  $m(\sigma)$  by

$$K H_0 + H_0 K^* = -G_0, \quad a_0 = H_0 a, \quad M(\sigma) = \int_0^\sigma \exp \left[ K \int_\tau^\sigma \frac{d\sigma_1}{\varphi(\sigma_1)} \right] d\tau, \quad \checkmark$$

$$m(\sigma) = \frac{1}{\varphi^2(\sigma)} K M(\sigma) a_0$$

Assume that for an  $\epsilon_0 > 0$  and all  $\sigma$  it holds

$$(3) \quad 1 - (G_0^{-1} m(\sigma), b) - \sqrt{(G_0^{-1} m(\sigma), m(\sigma)) \cdot (G_0^{-1} b, b)} \geq \epsilon_0 > 0$$

For the stability of (1) in the large it is necessary and sufficient that

Card 2/ 5

Stability Conditions in the Large for  
Some Non-Linear Differential Equations of  
Automatic Control

84655

S/020/60/135/001/006/030  
C111/C222

for all  $\sigma$ ,  $-\infty < \sigma < +\infty$  it holds

$$(4) \quad 2 \int_{\sigma}^{\sigma} (a, M(\sigma) a_0) d\sigma \geq (H_0^{-1} M(\sigma) a_0, M(\sigma) a_0) .$$

Let  $K^{-1}(Ha - \frac{b}{2\gamma} - - u$ , where H is the real solution of the inequation

$$-\gamma(KH + HK^*) - \mu_0^2 K^{-1} (Ha - \frac{b}{2\gamma})(Ha - \frac{b}{2\gamma})^* K^{*-1} + \frac{1}{\gamma} (ba^*H + Hab^*) -$$
  
$$-\frac{1}{\gamma^2} bb^* > 0$$

X

with

$$(8) \quad \mu_0^2 = \max \varphi'(\sigma)^2, \quad -\infty < \sigma < +\infty .$$

Theorem 2: Assume that the conditional equations (cf. (Ref.6))  
Card 3/ 5

84655

Stability Conditions in the Large for  
Some Non-Linear Differential Equations of  
Automatic Control

S/020/60/135/001/006/030  
C111/C222

$$(9) -\xi(KU + UK^*) = \mu_0^2 uu^* + \frac{1}{\xi} (Kub^* + bu K^*)$$

$$U^a + Ku + \frac{b'}{2\xi} = 0,$$

where  $\mu_0^2$  is given by (8), have real solutions  $u, U = U^*$  for all vectors  $b'$  being sufficiently neighboring to  $b$ . For the stability of (1) in the large it is sufficient and necessary that

$$(10) U > 0, \quad [\xi + 2(u, a)] \int_0^\sigma \varphi(\tau) d\tau \geq (U^{-1} u, u) \varphi(\sigma)^2$$

is satisfied.

Theorem 3: contains stability conditions for the case where the coefficients of (1) depend on a parameter.

Theorem 4 is a rougher modification of theorem 3 which is more convenient for stability control.

The assumptions of the theorems 1 - 4 are always satisfied if  $\xi$  is sufficiently large.

Card 4/5

Stability Conditions in the Large for  
Some Non-Linear Differential Equations of  
Automatic Control

84655

S/020/60/135/001/006/030  
C111/C222

The author mentions Ayzerman, Ye.A. Barbashin, N.N. Krasovskiy and Lyapunov. There are 6 Soviet references.

ASSOCIATION: Leningradskiy gosudarstvennyy universitet imeni A.A. Zhdanova  
(Leningrad State University imeni A.A. Zhdanov)

PRESENTED: June 6, 1960, by V.I. Smirnov, Academician

SUBMITTED: May 23, 1960

Card 5/5



YAKUBOVICH, V. A., and KRETIN, M. G.

"Hamiltonian systems of linear differential equations with periodic coefficients."

report submitted for the Intl. Symposium on Nonlinear Vibrations, IUPAM  
Kiev 12-18 Sep 1961

Acad. Sci. Ukr SSR

16.3400

22413  
S/042/61/016/001/007/007  
C 111/ C 333

AUTHOR: Yakubovich, V. A.  
TITLE: Systems of linear differential equations of canonical form with periodic coefficients (Autoreview of the dissertation)  
PERIODICAL: Uspekhi matematicheskikh nauk, v. 16, no. 1, 1961, 223-234

TEXT: The dissertation has been maintained on June 11, 1959 at the session of the Uchenyy sovet matematiko-mekhanicheskogo fakul'teta Leningradskogo universiteta (Scientific Council of the Mathematical-Mechanical Faculty of the Leningrad University). Opponents: V. J. Smirnov, Academician; M. G. Kreyn, Corresponding Member of the Academy of Sciences, UkrSSR; G. Yu. Dzhanelidze, Doctor of Physicomathematical Sciences; M. A. Krasnosel'skiy, Doctor of Physicomathematical Sciences. X

The results have been published by the author in (Ref. 17: Otsenka kharakteristicheskikh pokazateley sistemy lineynykh differentsial'nykh uravneniy s periodicheskimi koeffitsientami [Estimates of characteristic exponents of a system of linear differential equations  
Card 1/9

22413

S/042/61/016/001/007/007

C 111/ C 333

Systems of linear differential ...

with periodic coefficients], PMM 18, vyp. 4 (1954)); (Ref. 18: Rasprostraneniye metoda Lyapunov opredeleniya organichennosti resheniy uravneniya  $y'' + p(t)y = 0$ ,  $p(t+w) = p(t)$  na sluchay znakovremennoy funktsii  $p(t)$  [Extension of Lyapunov's method of determining boundedness of solutions of the equation  $y'' + p(t)y = 0$ ,  $p(t+w) = p(t)$  to the case of a function  $p(t)$  of variable sign.] PMM 18, vyp. 6 (1954)); (Ref. 19: O sistemakh differentsial'nykh uravneniy kanonicheskogo vida s periodicheskimi koeffitsientami poryadka bol'she dvukh [On systems of differential equations of canonical form with periodic coefficients of order  $> 2$ ] DAN 103, No. 6 (1955)); (Ref. 20: O zavisimosti sobstvennykh znacheniy samosopryazhennykh krayevykh zadach dlya sistemy dvukh differentsial'nykh uravneniy ot krayevykh usloviy [On the dependence of the eigenvalues of the boundary problem for the system of two differential equations on boundary conditions] Vestn. LGU, ser. matem. mekh. i astr., No. 1, vyp. 1 (1957)); (Ref. 21: Rasprostraneniye nekotorykh rezul'tatov Lyapunova na lineynyye kanonicheskiye sistemy s periodicheskimi koeffitsientami [Extension of some results of Lyapunov to linear canonical systems with periodic coefficients,] PMM 21, vyp. 4 (1957)); (Ref. 22: Zamechaniye k nekotorym

Card 2/3

22413

S/042/61/016/001/007/007

C 111/ C 333

Systems of linear differential ...

rabotam po sistemam lineynykh differentsial'nykh uravneniy s periodicheskimy koeffitsientami [Remarks on some papers on linear systems of differential equations with periodic coefficients], PMM 21, vyp. 5 (1957)); (Ref. 23: Stroyeniye gruppy simplekticheskikh matrits i i struktura mnozhestva neustoychivyykh kanonicheskikh sistem differentsial'nykh uravneniy s periodicheskimi koeffitsientami [Structure of the group of symplectic matrices and of the set of unstable canonical systems with periodic coefficients], Matem. sb. 44 (86): 3(1958)); (Ref. 24: Kriticheskiye chastoty kvazikanonicheskikh sistem [Critical frequencies of quasicanonical systems], Vestn. LGU 13, vyp. 3 (1958)); (Ref. 25: Ostsillyatsionnyye svoystva resheniy lineynykh kanonicheskikh uravneniy [Oscillation properties of solutions of linear canonical equations], DAN 123, No. 3 (1959)); (Ref. 26: Method malogo parametra dlya kanonicheskikh sistem s periodicheskimi koeffitsientami [Method of the small parameter for canonical systems with periodic coefficients], PMM 23, vyp. 1 (1959)); (Ref. 27: Voprosy ustoychivosti resheniy sistemy dvukh lineynykh differentsial'nykh uravneniy kanonicheskogo vida s periodicheskimi koeffitsientami [Questions of the stability of solutions of a

Card 3/9

22413

S/042/61/016/001/007/007

C 111/ C 333

Systems of linear differential ...

system of two linear differential equations of canonical form with periodic coefficients [7, Matem. sb. 37 (79), vyp. 1 (1955)].

X

A report on the results was given among others in the seminars of V. J. Smirnov, Academician (Leningrad); N. G. Chetayev, Corresponding Member of the Academy of Sciences USSR, Institut mekhaniki AN SSSR (Institute of Mechanics AS USSR); L. S. Pontryagin, Academician (MJAN); V. V. Nemytskiy, Professor (MGU).

The author considers the systems

$$\frac{dx}{dt} = JH(t) x \tag{2}$$

where x is a column vector with the components  $p_1, \dots, p_k, q_1, \dots, q_k$

$$H(t) = \begin{pmatrix} \|\alpha_{jh}\| & \|\beta_{hj}\| \\ \|\beta_{jh}\| & \|\gamma_{jh}\| \end{pmatrix} \quad j, h = 1, \dots, k, \quad J = \begin{pmatrix} 0 & I_k \\ -I_k & 0 \end{pmatrix}$$

Card 4/

22413

S/042/61/016/001/007/007

C 111/ C 333

Systems of linear differential ...

$I_k$  -- unit matrix. The  $\alpha, \beta, \gamma$  are real functions of  $t$  and integrable according to Lebesgue;  $\alpha_{jh}(t) = \alpha_{hj}(t)$ ,  $\gamma_{jh}(t) = \gamma_{hj}(t)$  almost everywhere.

Chapter I considers the structure of the space  $L = \{H(t)\}$  of all  $H(t) = H(t+\tau)$ , to which there correspond solutions of (2) which have certain properties. E. g. let  $\mathcal{M}$  be the set of the  $H(t)$  for which (2) possesses a certain number of bounded solutions for  $t \rightarrow \infty$ , while the other solutions are estimated by

$\|x(t)\| \leq C e^{\alpha t}$ ; these properties are said to be stable with respect to small variations of  $H(t)$ . It is stated that the sets  $\mathcal{M}$  thus defined are either domains or are decomposed into at most denumerably many domains. The author gives clear models of the space  $L$  for  $k = 1$  and  $k = 2$ . X

In chapter II the author considers the convex properties of the stability domains in  $L$ ; here  $\mathcal{M}$  is a stability domain, if the solutions of (2), the  $H(t)$  of which belongs to  $\mathcal{M}$ , are stable.  $\mathcal{M} \subset L$  is called convex in the direction of growth, if from

Card 5/9

22413  
S/042/61/016/001/007/007  
C 111/ C 333



Systems of linear differential ...

$H_1 \in \mathcal{M}_1, H_2 \in \mathcal{M}, H_1 \leq H_2$  it follows  $H \in \mathcal{M}$ , if  $H_1 \leq H \leq H_2$ .

It is stated that all stability domains are convex in this sense for  $k = 1, 2$ . Under certain assumptions the stability domains can be subdivided into convex subdomains for  $k > 2$ . These properties are used for obtaining sufficient stability conditions for (2).

In chapter III the author extends the Lyapunov method for the investigation of the Hill equation

$$\frac{d^2 y}{dt^2} + p(t) y = 0, p(t + \tau) = p(t) \tag{4}$$

to more general classes of canonical equations.

In chapter IV the author considers systems (2), the coefficients of which are not periodic. He investigates oscillation properties of the solutions and degenerated self-adjoint boundary value problems. A geometric definition of the oscillation character of the equation (2) is given, where results of J. M. Gelfand and V. B. Lidskiy

Card 6/9

22413

S/042/61/016/001/007/007

C 111/ C 333

Systems of linear differential ...

(Ref. 10: O strukture oblastey ustoychivoski kanonicheskikh lineynykh sistem differentsial'nykh uravneniy s periodicheskimi koeffitsientami [On the structure of the regions of stability of linear canonical systems of differential equations with periodic coefficients], UMN 10, vyp. 1 (63), (1955), 3-40) are essentially used. Degenerated self-adjoint boundary value problems are investigated for the equation

$$\frac{dx}{dt} = J(H_0(t) + \lambda H_1(t)) x \quad (6)$$

The author gives necessary and sufficient conditions for the existence of at least one and of an infinite number of eigenvalues tending to infinity.

Chapter V and VI have applied character. The author investigates the equation

$$\frac{dx}{dt} = J [H_0 + \epsilon H(\theta t, \epsilon)] x \quad (8)$$

where  $\theta$  is the exciting frequency and  $H(s, \epsilon) = H_1(s) + \epsilon H_2(s) + \dots$  ;

Card 7/9



22413

S/042/61/016/001/007/007  
C 111/ C 333

Systems of linear differential ...

especially the case of resonance is considered, where  $JH_0$  possesses eigen values which are congruent mod  $i0$ . The author describes parameter resonance and the construction of the dynamical instability domains of (8).

In a longer footnote the author rejects the objections of N. P. Yerugin who criticizes in (Ref.38: Metody issledovaniya sistem lineynykh differentsial'nykh uravneniy s periodicheskimi koeffitsientami [Methods of investigation of linear systems of differential equations with periodic coefficients]), Inzh.-fiz. zhurn. AN BSSR 3, No. 2 (1960) that the author uses results of other authors without reference in chapter 5 of his dissertation.

A. M. Lyapunov, L. D. Nikolenko, J. M. Glazman, N. N. Bogolykhov, Yu. A. Mitropol'skiy, J. Z. Shtokalo, J. G. Malkin and K. A. Breus are mentioned.

There are 44 Soviet-bloc and 2 non-Soviet-bloc references. The reference to English-language publication reads as follows:  
Card 8/9

Systems of linear differential ...

22413,  
S/042/61/016/001/007/007  
C 111/ C 333

R. Sternberg, Variational methods and non-oscillation theorems for systems of differential equations, Duke Math. Journ. 19, No. 2 (1952), 311-312.

Card 9/9

X

29024

S/043/61/000/004/002/008  
D274/D302

16.3400

AUTHOR: Yakubovich, V.A.

TITLE: Unbounded-stability conditions for a second-order differential equation

PERIODICAL: Leningrad. Universitet. Vestnik. Seriya matematiki, mekhaniki i astronomii, no. 4, 1961, 83 - 91

TEXT: Several theorems on unbounded stability of dynamical systems are proved. The equation

$$\frac{d^2x}{dt^2} + \nu \frac{dx}{dt} + \varphi(\theta t)x = 0 \tag{1.1}$$

is considered, where  $\nu > 0$ ,  $\theta > 0$ ,  $\varphi(s + 2\pi) = \varphi(s)$ , the function  $\varphi$  being either continuous on the interval  $[0, 2\pi]$  or having a finite number of singularities and

$$\int_0^{2\pi} |\varphi(s)| ds < \infty.$$

Card 1/6

Unbounded-stability conditions ...

29021  
S/048/61/000/004/002/008  
D274/D302

In the following, such functions are called  $2\pi$ -periodic, piecewise linear and integrable. According to M.A. Ayzerman (Ref. 1: Dostatochnoye usloviye ustoychivosti odnogo klassa dinamicheskikh sistem s peremennymi parametrami. PMM, v. 15, no. 3, 1951), a dynamic system described by Eq. (1.1) has unbounded stability if for any positive  $\theta$ , the condition

$$x(t) \rightarrow 0, \quad \frac{dx}{dt} \rightarrow 0 \text{ for } t \rightarrow +\infty \quad (1.2)$$

is satisfied. Another author considered Eq. (1.1) with piecewise-constant functions

$$\varphi(s) = \begin{cases} M^2 & \text{for } 0 < t < \pi, \\ m^2 & \text{for } \pi < t < 2\pi; \end{cases}$$

he arrived at the conditions

$$v^2 > \frac{M^2}{2} \left(1 - \frac{\sigma}{M} \sqrt{2 - \frac{\sigma^2}{M^2}}\right) \quad (1.3)$$

Card 2/6

Unbounded-stability conditions ...

2902h  
S/043/61/000/004/002/008  
D274/D302

where

$$\sigma^2 = \frac{1}{2} (m^2 + M^2).$$

A more general result can be derived from the author (Ref. 3: DAS SSSR, 87, 3, 1952). This result is formulated as Theorem 1: Denote by  $\Phi_{M,\sigma}$  the set of  $2\pi$ -periodic piecewise-linear, integrable functions  $\varphi(s)$  for which

$$\max \varphi(s) = M^2, \quad \frac{1}{2\pi} \int_0^{2\pi} \varphi(s) ds = \sigma^2 \geq 0$$

are preassigned numbers. For unbounded stability of Eq. (1.1) with any function  $\varphi(s) \in \Phi_{M,\sigma}$ , it is necessary and sufficient that inequality (1.3) hold. Below, a very simple direct proof of theorem 1 is given. An analogous result is formulated in a more elaborate way, when  $\min \varphi(s)$  is pre-assigned instead of  $\max \varphi(s)$ , viz. Theorem 2: Denote by  $\Psi_{m,\sigma}$  the set of functions  $\varphi(s)$  for which

Card 3/6

Unbounded-stability conditions ...

2902h  
S/043/61/000/004/002/008  
D274/D302

$$\min \varphi(s) = m^2, \quad \frac{1}{2\pi} \int_0^{2\pi} \varphi(s) ds = \sigma^2$$

are pre-assigned. In order that Eq. (1.1) have unbounded stability for any function  $\varphi(s) \in \Psi_{m, \sigma}$ , it is necessary and sufficient that

41

1) for  $\nu < m$ , inequality

$$\operatorname{ch} \frac{\nu \xi}{\sqrt{m^2 - \nu^2}} + \cos \xi - \frac{1}{2} \left( \frac{\sigma^2 - m^2}{m^2 - \nu^2} \right) \xi \sin \xi > 0 \quad (1.4)$$

should hold for any  $\xi$ ,  $0 < \xi < \pi$ ; 2) for  $\nu = m$ , inequality

$$\nu^2 \geq \frac{y_0}{1 + y_0} \sigma^2 = 0.50547 \dots \sigma^2 \quad (1.5)$$

should hold, where  $y_0 = 2x_0^2 \sqrt{x_0^2 - 1} (x_0 - \sqrt{x_0^2 - 1})$  and  $x_0 = 1.1996 \dots$ , is the solution of equation  $x = \operatorname{cthx}$ ; 3) for  $\nu > m$  inequality

Card 4/6

Unbounded-stability conditions ...

29024  
S/043/61/000/004/002/008  
D274/D302

$$\operatorname{ch} \frac{\nu \xi}{\sqrt{\nu^2 - m^2}} + \operatorname{ch} - \frac{1}{2} \left( \frac{\sigma^2 - m^2}{\nu^2 - m^2} \right) \xi \operatorname{sh} \xi > 0 \quad (1.6)$$

holds for any  $\xi > 0$ . Further, the analogous problem of evaluating the characteristic exponents of equation (1.1) which belong to the classes of functions  $\Phi_{m,\sigma}$  and  $\Psi_{m,\sigma}$ , is considered. As this problem is equivalent to evaluating the characteristic exponents for Hill's equation

$$\frac{d^2 y}{dt^2} + p(\theta t)y = 0, \quad (1.7)$$

the latter equation is considered, whereby the function  $p$  can also take negative values. Two theorems are formulated. Theorem 3: In order that for any positive  $\theta$  and  $p(s)$ , the approximation

$$y = O(e^{\mu t}), \quad t \rightarrow +\infty \quad (1.8)$$

to the solution of Eq. (1.7) should hold ( $\mu > 0$  being a pre-assi-  
Card 5/6

2902h  
S/043/61/000/004/002/008  
D274/D302

Unbounded-stability conditions ...

gned number). it is necessary and sufficient that

$$\mu \geq \begin{cases} \frac{p_{\max} - p_{cp}}{2 \sqrt{p_{\max}}} & \text{for } p_{\max} + p_{cp} > 0 \\ \sqrt{-p_{\max}} & \text{for } p_{\max} + p_{cp} < 0 \end{cases} \quad (1.9) \quad \text{41}$$

hold. Theorem 4 is analogous to theorem 2. In the following, the 4 theorems are proved. There are 10 references: 9 Soviet-bloc and 1 non-Soviet-bloc.

Card 6/6



LEVIN, Yu.V.; LYAPIN, Yo.S.; YANDEVICH, V.A.

Vladimir Abranovich Tartakovskii on his 60th birthday. Mat. nauk 16 no.5:225-230 S-O '61. (MEM 17:10)  
(Tartakovskii, Vladimir Abranovich, 1901-)

YAKUBOVICH, V.A.

Conditions of unlimited stability for a certain differential  
equation of the second order. Vest. LGU 16. no. 19:83-92 '61.

(MIRA 14:10)

(Differential equations)

16.3400

31906  
S/034/61/055/003/002/004  
D299/D304

AUTHOR: Yakubovich, V.A. (Leningrad)

TITLE: Arguments on a group of symplectic matrices

PERIODICAL: Matematicheskiy sbornik, v. 55, no. 3, 1961, 255-280

TEXT: The group of symplectic matrices is related to the linear system of canonical differential equations

$$p_j = \frac{\partial H}{\partial q_j}, \quad q_j = -\frac{\partial H}{\partial p_j} \quad (j = 1, \dots, k) \quad (0.1)$$

where H is a quadratic form of  $p_j, q_j$ , with real coefficients. The concept of argument on a group of symplectic matrices was introduced by I.M. Gel'fand and V.B. Lidskiy in connection with the structure of stability regions of Eq. (0.1) with periodic coefficients (Ref. 1: O strukture oblastey ustoychivosti lineynykh kano-nicheskikh sistem differentsial'nykh uravneniy s periodicheskimi koefbitsiyentami, Uspekhi matem. nauk, v. 10, no. 1 (63), 1955, 3

Card 1/6

X

31906

S/039/61/055/003/002/004  
D299/D304

Arguments on a group of ...

- 40). Various definitions of the argument are given, each of the definitions leading to some new interpretation of the number of stability- and instability regions of Eq. (0.1) with periodic coefficients. The main application of the arguments consists in studying the oscillatory properties of the solutions to Eq. (0.1); this however, is the subject of a later article by the author. The present article is devoted to defining the various arguments, their properties and their equivalence. Let  $\text{Arg}X$  be a real function (of even sign) of the matrix  $X \in G$ , satisfying the conditions: 1) The function  $\text{Arg}X$  is defined for any matrix  $X \in G$ ; 2) If  $(\text{Arg}X)_0$  denotes one of the values of  $\text{Arg}X$ , then the other values are

$$(\text{Arg}X)_m = (\text{Arg}X)_0 + 2m\pi \quad (m = \pm 1, \pm 2, \dots);$$

- 3) Each of the values  $(\text{Arg}X)_m$  is a continuous function of  $X \in G$ ;  
4) There exists a closed curve  $U(t) \in G$  with index unity, so that  $\Delta \text{Arg}U(t) = 2\pi$ . Any function which satisfies the above 4 conditions is called argument on the group of symplectic matrices. This defi-

Card 2/6

31906

S/039/61/055/003/002/004  
D299/D304

Arguments on a group of ...

dition can be rephrased: Assume a continuous mapping is given of the group  $G$  on a circle, whereby a closed curve  $U(t) \in G$ ,  $0 \leq t \leq 1$ , of index unity exists, so that if  $t$  varies from 0 to 1, the corresponding point traverses the circle once in the positive sense; by definition,  $\text{Arg} X$  is the argument (in the ordinary sense of the word) of the point on the circle, onto which the matrix  $X$  is mapped. A theorem is proved which shows that the various arguments defined above are equivalent in a topological sense. Assume, further

$$\text{Arg}_* X = \sum_{j=1}^k \text{Arg } \rho_j^{(+)}; \quad (1.7) \quad X$$

the matrix  $X$  is divided into 4  $k \times k$  -matrices:

$$X = \begin{pmatrix} U_1 & U_2 \\ V_1 & V_2 \end{pmatrix}; \quad (1.8)$$

the notations  
Card 3/6

31906

S/039/61/055/003/002/004  
D299/D304

Arguments on a group of ...

$$\left. \begin{aligned} \text{Arg}_1 X &= \text{Arg det } (U_1 - iV_1), \\ \text{Arg}_2 X &= \text{Arg det } (U_2 - iV_2), \\ \text{Arg}_3 X &= \text{Arg det } (U_1 + iU_2), \\ \text{Arg}_4 X &= \text{Arg det } (V_1 + iV_2), \end{aligned} \right\} \quad (1.9)$$

are introduced. It is also possible to take as arguments the functions X

$$\left. \begin{aligned} \text{Arg}'_{AB} X &= \text{Arg det } (U' - iV'), \\ \text{Arg}''_{AB} X &= \text{Arg det } (U'' + iV''). \end{aligned} \right\} \quad (1.11)$$

Theorem 3. Each of the functions defined by formulas (1.7), (1.9) and (1.11), satisfies the conditions of the definition and can, therefore, be considered as an argument on the group of symplectic matrices. The equivalence of various definitions is then examined. Let Arg'X and Arg''X be two different arguments, i.e. two functions on G which satisfy the 4 conditions of the definition. The arguments Arg'X and Arg''X are called equivalent if a positive constant

Card 4/6

31906  
S, 039/61/055/003/002/004  
D299/D304

Arguments on a group of ...

C exists, so that for any continuous curve  $X(t) \in G$ , the inequality

$$|\Delta \text{Arg}'X(t) - \Delta \text{Arg}''X(t)| < C$$

holds. Further, a model is constructed which shows that various arguments, both equivalent and non-equivalent can be introduced which satisfy the 4 conditions of the definition. Theorem 4. The above-introduced arguments

$\text{Arg}_j X$  ( $j = 0, 1, 2, 3, 4$ ),  $\text{Arg}'_{AB} X$ ,  $\text{Arg}''_{AB} X$ ,  $\text{Arg}_* X$ ,

are equivalent. This theorem is important for studying the oscillatory properties of the solution to Eq. (0.1). Its proof is complicated and involves several lemmas. There are 3 figures and 20 references: 14 Soviet-bloc and 6 non-Soviet-bloc, (including 3 translations). The references to the English-language publications read as follows: R.L. Sternberg, Variational methods and non-oscillation theorems for systems of differential equations, Duke Math. Journ. 19, no. 2, 1952, 311-322; W.T. Reid, The theory of the second variation for non-parametric problem of Bolza, Amer.

Card 5/6

Arguments on a group of ...

31906  
S/039/61/055/003/002/004  
D299/D304

Journ. Math., 57, 1935, 573-586; W.T. Reid, A matrix differential equation of Riccati type, Amer. Journ. Math., 68, 1946, 237-246. x

SUBMITTED: January 7, 1960

Card 6/6



YAKUBOVICH, V.A.

Structure of the functional space of complex canonical equations  
with periodical coefficients. Dokl. AN SSSR 139 no.1:54-57 J1  
'61. (MIRA 14:7)

1. Leningradskiy gosudarstvennyy universitet im. A.A Zhdanova.  
Predstavleno akademikom V.I. Smirnovym.  
(Differential equations) (Groups, Theory of)

YAKUBOVICH, V.A.

Convex properties of the stability domains of linear Hamiltonian systems of differential equations with periodic coefficients.  
Vest. IGU 17 no.13:61-86 '62. (MIRA 15:7)  
(Differential equations, Linear)

GEL'FOND, A.O.; LINNIK, Yu.V.; CHUDAKOV, N.G.; YAKUBOVICH, V.A.; LINNIK,  
IU.V.; CHUDAKOV, N.G.; IAKUBOVICH, V.A.

An incorrect work of N.I.Gavrilov. Usp.mat.nauk 17 no.1:265-267  
Ja-F '62. (MIRA 15:3)

(Functions, Zeta)  
(Gavrilov, N.I.)

16.3400

31909  
S/039/62/056/001/001/003  
B112/B138

AUTHOR: Yakubovich, V. A. (Leningrad)

TITLE: Oscillation properties of the solutions of canonical equations

PERIODICAL: Matematicheskiy sbornik, v. 56(98), no. 1, 1962, 3-42

TEXT: The author studies the oscillation properties of the solutions of the canonical system  $Jdx/dt = H(t)x$ , where

$$J = \begin{pmatrix} 0 & -I_k \\ I_k & 0 \end{pmatrix}$$

and  $H(t) = H^*(t)$ . The method applied is a geometric rather than an analytic one. It is based on the fact that each fundamental solution matrix  $X(t)$  is a symplectic matrix:  $X^*JX = J$ . The symplectic group  $G = \{X\}$  has the topological structure of a multi-dimensional torus. This result is due to I. M. Gel'fand and V. B. Lidskiy (Uspekhi matem. nauk, t. X, vyp. 1(63) (1955), 3- 40.). The canonical system considered is said  
Card 1/3

X

31909

S/039/62/056/001/001/003  
B112/B138

Oscillation properties of the ...

to be of the oscillation type if the fundamental matrix  $X(t)$  "rotates" without limitation on the torus  $G$  for  $t \rightarrow +\infty$ . The equivalence of different definitions of oscillation is shown. A series of criteria are derived for whether a given canonical system is of the oscillation type or not. G. A. Bliss (Lektsii po variatsionnomu ischisleniyu, Moscow, IIL, 1950.), I. M. Glazman (DAN SSSR, t. 118, No. 3 (1958), 423 - 426., t. 119, No. 3 (1958), 421 - 424.), V. A. Kondrat'yev (Uspokhi matem. nauk, t. XII, vyp. 2 (75) (1957), 159 - 160., Trudy Mosk. matem. o-va, t. 8 (1959), 259 - 282.), L. D. Nikolenko (Avtoreferat dissertatsii, Kiyev, 1956.; DAN SSSR, t. 110, No. 6 (1956), 929 - 931.), M. G. Kreyn (DAN SSSR, t. 73, No. 3 (1950), 445 - 448.), V. B. Lidskiy (DAN SSSR, t. 102, No. 5 (1955), 877 - 880.) are referred to. There are 4 figures and 34 references: 26 Soviet and 8 non-Soviet. The four most recent references to English-language publications read as follows: R. L. Sternberg, Variational methods and non-oscillation theorems for systems of differential equations, Duke Math. Journ., 19, No. 2 (1952), 311 - 322; J. H. Barrett, A Prüfer transformation for matrix differential equations, Proc. Amer. Math. Soc., 8, No. 3 (1957), 510 - 518; W. T. Reid, The theory of the second variation for non-parametric problem of Bolza, Amer. Journ. Math., 57 (1935), 573 - 586; W. T. Reid, A matrix differential equation of

Card 2/3

X

Oscillation properties of the ...

<sup>31909</sup>  
S/039/62/056/001/001/003  
B112/B138

Riccati type, Amer. Journ. Math., 68 (1946), 237 - 246.

SUBMITTED: January 7, 1960

✓

Card 3/3

16.8000  
16.1500

37378  
S/020/62/143/006/007/024  
B125/B112

AUTHOR: Yakubovich, V. A.

TITLE: Solution of a few matrix inequalities in the automatic control theory

PERIODICAL: Akademiya nauk SSSR. Doklady, v. 143, no. 6, 1962, 1304-1307

TEXT: The author derives a necessary and sufficient condition under which a Hermitean matrix  $H = H^*$  exists for a given matrix  $A$  and for given vectors  $a$  and  $b$ , so that the matrix  $G - gg^*$ , where  $G = -(A^*H + HA)$ , and  $g = -(Ha+b)$ , is positive definite. This condition reads  $1 + 2\text{Re} ((A-i\omega)^{-1} a, b) > 0$  for  $-\infty < \omega < +\infty$ . The formulation of the problem is connected with problems concerning the optimum conditions of stability for nonlinear differential equations. The most important English-language reference is: S. Lefschetz, RIAS technical report 60-9, 1960.

PRESENTED: December 11, 1961, by V. I. Smirnov, Academician

SUBMITTED: December 11, 1961

Card 1/1

L 15573-63

ACCESSION NR: AT3002555

ENT(a)/FCC(w)/BDS

AFFTC LJP(C)

S/2944/63/000/001/0030/0044

AUTHOR: Yakubovich, V. A.

53

TITLE: Two-sided estimates of the solution of a homogeneous second order differential equation

SOURCE: Leningrad, Universitet. Kafedra vychislitel'noy matematiki i Vychislitel'nyy tsentr. Metody vychisleniy, no. 1, 1963, 30-44

TOPIC TAGS: differential equation, inequality, upper bound, lower bound, region of parameter value

ABSTRACT: The author considers the equation

$$\frac{d^2x}{dt^2} + P(t) \frac{dx}{dt} + Q(t)x = 0 \tag{1}$$

subject to the initial conditions  $x(0) = x_0, x'(0) = x'_0$ , where the coefficient functions in (1) depend upon parameters  $\alpha_1, \dots, \alpha_m$ . He wishes to find a set of parameter values for which

Card 1/6

$$x(T) < x' \quad \text{or} \quad x(T) > x' \tag{2}$$



L 15573-63

ACCESSION-NR: AT3002555

He also would like to find an increasing sequence of such sets whose union is the set of all such parameter points. By the usual reduction, he transfers (1) and (2) to

$$\frac{d^2y}{dt^2} + p(t)y = 0. \quad (3)$$

$$y(0) = a, \quad \dot{y}(0) = b \quad (4)$$

He attempts to accomplish the desired result by the natural use of sequences  $v^{(n)}$ ,  $w^{(n)}$ , satisfying

$$\begin{aligned} \text{(I)} \quad & v^{(n)}(t) < y(t) \leq w^{(n)}(t), \\ \text{(II)} \quad & v^{(1)}(t) < v^{(2)}(t) \leq \dots, \quad w^{(1)}(t) > w^{(2)}(t) > \dots \end{aligned} \quad (5)$$

(III) for  $n \rightarrow \infty$  uniformly in  $t \in (0, T)$  the following is satisfied  $v^{(n)}(t) \rightarrow y(t)$ ,  $w^{(n)}(t) \rightarrow y(t)$ .

Such sequences are constructed typically by the use of Theorem 1. Assume  $p(t)$  to be the form

$$p(t) = p_0(t) + p_1(t), \quad (6)$$

Card 2/6

L 15573-63

ACCESSION NR: AT3002555

0

where  $p_0(t), p_1(t) \in L_2(0, T)$ , and such that the following conditions are satisfied:

a)  $p_1(t) \geq 0$  for  $0 \leq t \leq T$  and the measure of the set  $\{t: 0 \leq p_1(t) < \epsilon\}$  tends to 0 as  $\epsilon \rightarrow 0$ ;

b) we know the fundamental system of solutions  $u_1(t), u_2(t)$  of the equation

$$\frac{d^2u}{dt^2} + p_0(t)u = 0 \tag{7}$$

with initial conditions

$$\begin{pmatrix} u_1 & u_2 \\ \dot{u}_1 & \dot{u}_2 \end{pmatrix}_{t=0} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \tag{8}$$

c) within the given interval  $(0, T)$  the function  $u_2(t)$  has no zero.

If

$$p(t) > c_0 \quad \text{for} \quad 0 \leq t < T, \tag{9}$$

Card 3/6

L 15573-63

ACCESSION NR: AT3002555

then the conditions (a), (b), (c) can be satisfied, taking, for example, as  $p_0(t)$ , any function  $p_0(t) = c$ , where the constant  $c$  is subject to the condition

$$c \leq \min [c_0, \pi^2/T^2]. \quad (10)$$

As the "zero approximation" the author takes the solution  $u = y_0(t)$  of equation (7) with initial conditions (4).

Theorem 1. Assume that (a), (b) and (c) are satisfied and that  $y_0(t) > 0$  on  $(0, T)$ . Sequentially define the functions  $y_1(t), y_2(t), \dots$  from the equations

$$\frac{d^2 y_{n+1}}{dt^2} + p_0(t) y_{n+1} = p_1(t) y_n, \quad y_{n+1}(0) = 0, \quad y_{n+1}(T) = 0, \quad n = 0, 1, 2, \dots \quad (11)$$

and set

$$y^{(n)}(t) = y_0(t) - y_1(t) + \dots + (-1)^n y_n(t). \quad (12)$$

Card 4/6

L. 15573-63

ACCESSION NR: AT3002555

Then for  $0 < t < T$ :

1) all  $y_n(t) > 0$ ,  $n = 1, 2, \dots$ ,

$$\frac{y_{n+1}(t)}{y_n(t)} < \frac{n}{n+1} \frac{y_n(t)}{y_{n-1}(t)} \quad (13)$$

3) there exists an integer  $m = m(t) \geq 0$  such that

$$\begin{aligned} y_0(t) < y_1(t) < \dots < y_m(t), \\ y_m(t) > y_{m+1}(t) > y_{m+2}(t) > \dots \end{aligned} \quad (14)$$

4) if  $t' < t''$ , then  $m(t') \leq m(t'')$

5) for the solution  $y(t)$  of (3) with initial conditions (4)

$$\left. \begin{aligned} y(t) < y^{(n)}(t) & \text{ for even } n > m(t) - 1, \\ y(t) > y^{(n)}(t) & \text{ for odd } n > m(t) - 1, \end{aligned} \right\} \quad (15)$$

Card 5/6

L 15573-63

ACCESSION NR: AT3002555

6) if for even  $n$ ,  $y^{(n)}(t) \leq y_0(t)$  or for odd  $n$ ,  $y^{(n)}(t) \geq -y_0(t)$ , then  $n \geq m(t)$ .

7) as  $n \rightarrow +\infty$  uniformly in  $t \in [0, T]$

$$y^{(2n)}(t) \rightarrow y(t), \quad y^{(2n+1)}(t) \rightarrow y'(t).$$

Orig. art. has: 34 formulas and 3 figures.

(16)

ASSOCIATION: none

SUBMITTED: 00

DATE ACQ: 28Jun63

ENCL: 00

SUB CODE: MM

NO REF SOV: 005

OTHER: 001

Card 6/6

ACCESSION NR: AT4008597

S/2944/63/000/002/0095/0131

AUTHOR: Yakubovich, V. A.

TITLE: Machines learning to recognize images

SOURCE: Leningrad. Universitet. Kafedra vy\*chislitel'noy matematiki i vy\*chislitel'ny\*y tsentr. Metody\* vy\*chisleniy, no. 2, 1963, 95-131

TOPIC TAGS: image recognition machine, selflearning computer, computer, perceptron, character recognition machine, vowel recognition machine, linear perceptron

ABSTRACT: The characteristics of image recognizing machines (perceptrons), (the basic elements of which are identified as the retina, the associative element, the summing element, and the logical element), are described by methods of set theory with mathematical rigor, but the treatment is made understandable to the non-mathe-

Card 1/3

ACCESSION NR: AT4008597

matician. The subject headings are: Introduction. 1. Schematic diagram of the perceptron. 2. Diagram of the recognition block. Linear perceptron. 3. Perceptron with one summing element. 4. Concepts that can be distinguished by a perceptron with a single summing element. 5. Concerning one algorithm for the separation of convex sets. 6. Separation of an arbitrary number of generally non-convex sets. Learning block of a perceptron with many summing elements. 7. Description of the experiments performed. These cover the recognition of convex and concave functions, recognition of handwritten numbers, recognition of profiles, and recognition of vowel phonemes. "The author is grateful to the students M. Persiyanov, T. Bogdarin, and N. Belyayev for much work done in the experiments, and to Prof. G. V. Gershuni and Prof. L. A. Chistovich, who supplied the graphs for the vowels." Orig. art. has: 14 figures and 47 formulas.

ASSOCIATION: Leningradskiy gosudarstvennyy universitet (Leningrad

Card 2/3

ACCESSION NR: AT4008597

State University)

SUBMITTED: 00

DATE ACQ: 27Dec63

ENCL: 00

SUB CODE: CP

NO REF SOV: .008

OTHER: 004

Card 3/3



YAKUBOVICH, V.A. (Leningrad)

Absolute stability of nonlinear control systems in critical cases. Part 1. Avtom.1 telem. 24 no.3:293-303 Mr '63.

(MIRA 16:4)

(Automatic control)

L 10322-63 EWT(d)/BDS--AFFTC/APGC/ASD--

Pg-1/Pk-1/P1-1/Po-1/Pq-1--BC

ACCESSION NR: AP3001081

S/0103/63/024/006/0717/0731

AUTHOR: Yakubovich, V. A. (Leningrad)

72

TITLE: Absolute stability of nonlinear controlled systems in critical cases. 2

SOURCE: Avtomatika i telemekhanika, v. 24, no. 6, 1963, 717-731

TOPIC TAGS: stability of controlled systems, nonlinear controlled systems, Lyapunov's functions in automation

ABSTRACT: A theorem is proved that yields effective, necessary, and sufficient conditions for the existence of the Lyapunov's function -- "quadratic form plus an integral of nonlinearity" -- with a least degenerated derivative. Possibilities are explored of using such Lyapunov's functions in the problems with fixed nonlinearity. Pertinent formulas are given in Enclosure 1. Orig. art. has: 60 formulas.

ASSOCIATION: none

SUBMITTED: 03May62

DATE ACQD: 01Jul63

ENCL: 01

SUB CODE: 00

NO REF SOV: 015

OTHER: 001

Card 1/2

L 10322-63

ACCESSION NR: AP3001081

ENCLOSURE: 1

Automatic control system is described by these equations:

$$\frac{dx}{dt} = Ax + a\varphi(\sigma), \quad \frac{d\sigma}{dt} = b^*x - p\varphi(\sigma),$$

where the matrix A has eigenvalues in the left closed semiplane; any number of them can be on the imaginary axis. The continuous function satisfies the inequality

$$0 < \frac{\varphi(\sigma)}{\sigma} < \mu_0 \quad (\sigma \neq 0, 0 < \mu_0 < +\infty)$$

The fundamental problem is to find the conditions of absolute stability which would encompass all conditions expressed by a Lyapunov function of this type

$$V = (Hx, x) + 2(h, x)\sigma + \chi\sigma^2 + \vartheta \int_0^\sigma \varphi(\sigma) d\sigma$$

with a least degenerated derivative. Here  $H, h, \chi, \vartheta$  are some parameters.

Card 2/2 *rw/10/23*

S/020/63/149/002/008/028  
B112/B180

AUTHOR: Yakubovich, V. A.

TITLE: Frequency conditions for absolute stability of controllable systems with hysteresis non-linearities

PERIODICAL: Akademiya nauk SSSR. Doklady, v. 149, no. 2, 1963, 288-291

TEXT: Hysteresis operators  $\mathcal{Y}[\sigma, f_0]_t$  are considered which satisfy the following conditions: (1) For any  $\sigma_0$  there exists a set  $\mathcal{L}(\sigma_0)$  of initial values of hysteresis function. (2) The set  $\mathcal{M}_{\sigma_0}(t_0, t_1)$  of the continuous functions  $\sigma(t)$  with  $\sigma(t_0) = \sigma_0$  is mapped into the set  $\mathcal{C}(t_0, t_1)$  by the operator

$$\mathcal{Y} \left[ \begin{array}{c} t_1 \\ t_0, \sigma_0 \end{array} \right].$$

The equation

Card 1/2

Frequency conditions for absolute ...

S/020/63/149/002/008/028  
B112/B180

$$dz/dt + Pz + q\gamma[\sigma, \gamma_0]_t, \sigma = (z, r) \quad (1)$$

is shown to be solvable if  $\gamma[\sigma, \gamma_0]$  is a continuous operator. The case where  $\gamma[\sigma, \gamma_0]$  is discontinuous is an unsolved mathematical problem.

Conditions of absolute stability of Eq. (1) are derived: One of them is the following:  $0 \leq \sigma(t) \gamma[\sigma, \gamma_0]_t \leq \mu_0 \sigma(t)^2$ ;  $\gamma[\sigma, \gamma_0]_t = 0$  for  $\sigma(t) = 0$ ,

$\gamma(\omega) = 1/\mu_0 + \text{Re} \chi(i\omega) > 0$  for  $0 \leq \omega < \infty$  ( $\chi(\lambda) = ((P - \lambda I)^{-1} q r)$ ),

$\lim_{\omega \rightarrow \infty} \gamma(\omega) > 0$ . There is 1 figure.

PRESENTED: September 18, 1962, by V. I. Smirnov, Academician

SUBMITTED: September 15, 1962

Card 2/2

DERGUZOV, V.I.; YAKUBOVICH, V.A.

Existence of solutions to linear Hamiltonian equations with  
unbounded operator coefficients. Dokl. AN SSSR 151 no.6:1264-1267  
Ag '63. (MIRA 16:10)

1. Predstavleno akademikom V.I.Smirnovym.

YAKUBOVICH, V.A. (Leningrad)

Absolute stability of nonlinear controlled systems in critical  
cases. Part 3. Avtom. i telem. 25 no.5:601-612 My '64.  
(MIRA 17:9)

ACCESSION NR: AP4042487

S/0103/64/025/007/1017/1029

AUTHOR: Yakubovich, V. A. (Leningrad)

TITLE: Method of matrix inequalities in the theory of stability of nonlinear controlled systems. Part 1 - Absolute stability of forced oscillations

SOURCE: Avtomatika i telemekhanika, v. 25, no. 7, 1964, 1017-1029

TOPIC TAGS: automatic control, nonlinear automatic control, automatic control theory, automatic control stability

ABSTRACT: The existence and absolute stability of forced periodic and quasi-periodic oscillations in a controlled system having one nonlinearity are analyzed. This set of equations is considered:

$$dx/dt = Px + q\varphi(\sigma) + f(t), \quad \sigma = r^*x, \quad (1)$$

where  $f(t)$  is a vector function limited within  $(-\infty + \infty)$ ;  $\varphi(\sigma)$ , generally a discontinuous function, has only isolated points of discontinuity of the first kind. Any function  $x(t)$  can be a solution of the above set (1) provided a function  $\psi(t)$  satisfies these conditions:

Card 1/2



ACCESSION NR: AP4042487

$$dx/dt = Px + q\psi(t) + f(t),$$

$$\varphi_-(\sigma(t)) \leq \psi(t) \leq \varphi_+(\sigma(t)), \quad \sigma(t) = r'x(t).$$

Under certain assumptions regarding the roots (Theorem 1), the solution  $x_0(t)$  is exponentially stable in grossen with the exponent exceeding  $\alpha$ , i.e., such numbers  $\beta > 0$   $\xi > 0$  exist, that for any  $t \geq t_0$  and any solution  $x(t)$ , this inequality holds true:

$$|x(t) - x_0(t)| \leq \beta e^{-(\alpha+\xi)(t-t_0)} |x(t_0) - x_0(t_0)|.$$

Further, forced oscillations are investigated assuming that the solution  $x_0(t)$  is known. Among other things, it is found that, in the absence of external influences, the condition of absolute stability with a specified decrement is similar to V. M. Popov's condition. Orig. art. has: 50 formulas.

ASSOCIATION: none

SUBMITTED: 04Nov63

ENCL: 00

SUB CODE: DP, IE

NO REF SOV: 025

OTHER: 008

Card 2/2

STARZHINSKY, V.H. (Moscow); YAKUBOVICH, V.A. (Leningrad)

"Contribution to the Lyapunov method of determining periodic solutions"

Report presented at the 2nd All-Union Congress on Theoretical and Applied Mechanics, Moscow 29 Jan - 5 Feb 64.

GANTMAKHER, F.R. (Moscow); YAKUBOVICH, V.A. (Leningrad):

"Absolute stability of non-linear controls."

report presented at the 2nd All-Union Congress on Theoretical and Applied Mechanics, Moscow, 29 Jan - 5 Feb 64.

ACCESSION NR: AP4036716

8/0020/64/156/002/0278/0281

AUTHOR: Yakubovich, V. A.

TITLE: A solution for certain matrix inequalities encountered in a nonlinear control theory

SOURCE: AN SSSR Doklady\*, v. 156, no. 2, 1964, 278-281

TOPIC TAGS: matrix inequality, nonlinear control, Lyapunov function, matrix spectrum, closed halfplane, absolute stability, Lurie method, quadratic form

ABSTRACT: This paper deals with special systems of differential equations (e.g., for automatic control) and a bounded class of the Lyapunov function (e.g., quadratic forms). The existence of this function was converted into a purely algebraic problem involving the existence of a solution to certain specialized matrix inequalities. Through a series of mathematical arguments and the construction of theorems, a solution was presented. In his third theorem, the author assumes that  $\mu_0 \neq \infty$ .

Therefore, in order to have a matrix  $H = H^*$  in which  $F(\mu, H) > 0$  when  $0 \leq \mu \leq \mu_0$ , it is necessary that in the case of a certain  $\tau \geq 0$  and all  $\omega \geq 0$ , the following equation be carried out:

Card 1/2

ACCESSION NR: AF40.36716

$$\pi_1(\omega) \equiv \gamma + 2\text{Re } p^* (P - i\omega I)^{-1} q + \tau [\mu_0^{-1} + \text{Re } r^* (P - i\omega I)^{-1} q] > 0 \quad (4)$$

Orig. art. has: 6 equations, 4 theorems, and 1 lemma.

ASSOCIATION: none

SUBMITTED: 15Jan64

DATE ACQ: 03Jun64

ENCL: 00

SUB CODE: MA

NO REF SOV: 004

OTHER: 002

Card 2/2

ACCESSION NR: AP9016180

TR/0124 0010 10. A. A. 110

SOURCE: Izv. Akad. Nauk SSSR, Ser. Mekhanika, Abs. 6A13

AUTHOR: Yakubovich, V. A.

TITLE: Frequency conditions for the absolute stability of nonlinear automatic control systems

CITED SOURCE: Tr. Meshvuz. konferentsii po prikl. mekhan., 1962. Kazan', 1964, 135-142

TOPIC TAGS: nonlinear automatic control system, absolute stability, stability condition, Lyapunov function <sup>14</sup>

TRANSLATION: The controlled system is studied:  $\dot{x} = Px + q\Phi(\sigma)$ , where  $\sigma = r^*x$ , P is a constant Hurwitz matrix, q and r are constant columns, and the function  $\Phi$  satisfies the condition  $0 \leq \Phi(\sigma) \leq \mu\sigma^2$ ,  $\mu \ll +\infty$ . The solution of the matrix problem is formulated, on the basis of which the sufficient conditions V. A. Yakubovich for the absolute stability of the investigated system are derived by analysis of the Lyapunov function  $V = r^*Hx + \int_0^\sigma \varphi(\sigma) d\sigma$  (H is a positive-definite <sup>16</sup>

Card 1/2

L 58921-65

ACCESSION NR: AR5016489

matrix). It is shown that the obtained results are valid even in the case when  $\Phi(\sigma)$  is a piecewise-continuous function. The third matrix problem is cited, and it is shown that it is now solved. It follows from its solution that the "weak" condition of V. M. Popov is necessary for the existence of the Lyapunov function with  $U \ll 0$ . The frequency condition for absolute stability, is derived also for the case when  $\Phi$  is a continuous hysteresis function. A system with the piecewise-continuous function  $\Phi(\sigma)$ ,  $d\Phi/d\sigma \geq 0$  is also considered. A sufficient frequency condition for absolute system stability, broader than the condition of V. M. Popov, is obtained by analysis of the Lyapunov function. A. Kh. Gelig

SUB CODE: IE, MA

ENCL: 00

Card 2/2 *dm*

L 08829-67 EWT(d)/EWP(1) IJP(c) BB/GG  
 ACC NR: AT6022616 (A) SOURCE CODE: UR/3040/65/000/004/0003/0071

35

AUTHOR: Yakubovich, V. A.

ORG: none

TITLE: Some general theoretical principles for the construction of learning perception systems. I

SOURCE: Leningrad. Universitet. Kafedra vychislitel'noy matematiki i Vychislitel'nyy tsentr. Vychislitel'naya tekhnika i voprosy programirovaniya, no. 4, 1965, 3-71

TOPIC TAGS: information theory, perceptron, automaton

ABSTRACT: General principles are given for the construction of automatic systems which model human perception and identification processes. A large class of models of the perceptron type is discussed. A general introduction is given, describing the general properties of a perception system. The general formula for such a system is

$$s(x) \approx \sum_{j=1}^N x_j a_j(x).$$

where  $x_j$  are certain numerical coefficients,  $s(x)$  is an elementary "concept" resulting from the perception of image  $x$ , and  $a_j$  are certain so-called "a-elements"---functional

Card 1/2



L 08829-67

ACC NR: AT6022616

elements which react on incoming images. The method for choosing these  $a$ -elements is discussed. It is shown that the collection of functions representing  $a$ -elements is complete in the field of images under certain sufficiently general assumptions regarding the functions given on the receptor field ("retina"). It is shown also that for an optimal choice of coefficients  $x_j$ , the probability of error in perception will become arbitrarily small providing the number  $N$  of  $a$ -elements is sufficiently large, along with the number  $m$  of elements of the learning sequence. The requirements for an algorithm of learning and perception are discussed. Systems are studied which are based on the defined notions of  $L$ - and  $C$ -optimality. The  $L$ -algorithm is shown to be theoretically superior but extremely unwieldy and hence unsuitable for circuit form; while algorithms satisfying  $C$ -optimal requirements, converging only with sufficiently great values of  $N$ , are quite simple and can be circuit-programmed. These algorithms are recurrence solutions of linear inequalities and equations. Orig. art. has: 225 formulas, 9 figures, 1 table.

SUB CODE: 09,12/      SUBM DATE: 01Aug64/      ORIG REF: 017/      OTH REF: 006

Card 2/2      nst

EWT/4 ... EWP(k)/EWP(h)/EWP(1) P5-4/Pq-4/Pf-4/Pg-4/Pk-4/Pl-4  
ACCESSION NR: AP5011900 UR/0103/65/026/004/0577/0590

AUTHOR: Yakubovich, V. A. (Leningrad)

TITLE: The method of matrix inequalities in the theory of stability of nonlinear controlled systems. II. Absolute stability in a class of nonlinearities with derivative condition

SOURCE: Avtomatika i telemekhanika, v. 26, no. 4, 1965, 577-590

TOPIC TAGS: control system stability, nonlinear class stability, derivative condition, absolute nonlinear system stability, matrix inequality

ABSTRACT: The author studied the system

$$\frac{dx}{dt} = Px + q\varphi(\sigma), \quad \sigma = r^*x, \quad (1)$$

where  $\varphi(\sigma)$  is a function differentiable at every point and satisfying

$$0 \leq \sigma\varphi(\sigma) \leq \mu\sigma^2 \quad (\mu_0 \leq +\infty), \quad (2)$$

and either

$$\varphi'(\sigma) \leq a_1, \quad (3)$$

Card 1/2

L 48952-65  
ACCESSION NR: AP5011900

0

or

$$\varphi'(\sigma) \geq a_2. \tag{4}$$

and derived a new frequency condition for the absolute stability of the nonlinearity classes satisfying (2) and (3), or (2) and (4) and an additional condition  $a_2 > 0$ . In equation (1), Latin capital letters denote matrices, small letters denote scalars. The results obtained are generalizations of the corresponding results of [1]. In the present consideration, all the conditions are assumed to be satisfied for all  $\sigma$  in the interval  $0 < \sigma < \infty$ . The results obtained are based on the application of the integral over the semi-axis  $\sigma > 0$  of the matrix inequalities discussed earlier (Dokl. AN SSSR, v. 143, no. 6, 1962). An appendix contains the proof of four theorems used in the text. Orig. art. has 86 formulas and 1 figure.

ASSOCIATION: None

SUBMITTED: 23Sep63

NO REF SOV: 013

ENCL: 00

OTHER: 005

SUB CODE: IE, MA

Card 2/2

00-077.32

AUTHOR: Yakubovich, V. A. (Leningrad)

TITLE: Method of matrix inequalities in the theory of stability of nonlinear controlled systems. Part 3 - Absolute stability of systems having hysteresis-type nonlinearities

SOURCE: Avtomatika i telemekhanika, v. 26, no. 5, 1965, 753-763

TOPIC TAGS: nonlinear automatic control, automatic control, automatic control design, automatic control system, automatic control theory

ABSTRACT: The article proves that the V. M. Popov frequency condition holds true in the case of a hysteresis-type nonlinearity if the parameter that enters the above condition has a definite sign that depends on the direction of following the hysteresis loop. An automatic-control system is considered which can be

described by these equations:  $\frac{dx}{dt} = Px + q\sigma(\sigma, \varphi_0)$ ,  $\sigma = r'r$ , where  $P - \nu \times \nu$  is a

ACCESSION NR: AP5013832

constant matrix;  $q, r - \sqrt{x}$  are constant vectors ( $q \neq 0, r \neq 0$ );  $r^*x$  is a scalar product;  $\varphi[\sigma, \varphi_0]_t$  is a hysteresis function. For a backlash-type nonlinearity, the condition of absolute stability is determined. Orig. art. has: 3 figures and 55 formulas.

ASSOCIATION: none

SUBMITTED: 17Jul63

ENCL: 00

SUB CODE: DP, LE

NO REF SOV: 011

OTHER: 000

Card 2/2

AUTHOR: Yakubovich, V. A.

TITLE: Frequency criteria for absolute stability and dissipativity of control systems with one differentiable nonlinearity

SOURCE: AN SSSR. Doklady, v. 160, no. 2, 1965, 298-301

TOPIC TAGS: absolute stability criterion, dissipativity criterion, nonlinear control system, global asymptotic stability

ABSTRACT: A study is made of the stability of nonlinear control systems described by the system of differential equations

$$\dot{x} / dt = Px + q\varphi(\sigma), \tag{1}$$

where  $\sigma = r^*x$ ,  $P$  is a Hurwitz matrix,  $q$  is a vector, and  $\varphi(\sigma)$  is a differentiable function satisfying the following conditions:

$$a) 0 \leq \sigma\varphi(\sigma) \leq \mu\sigma^2; \quad b) -\alpha_1 \leq \varphi(\sigma) \leq \alpha_2 \tag{2}$$

Card 1/3

L 25383-65

ACCESSION NR: AP5004585

where  $u_0, a_1,$  and  $a_2$  are finite numbers. An expression  $w(\omega)$  containing certain parameters  $\tau_1, \tau_2, \theta,$  and the transfer function of the linear part of the system  $X(\omega)$  is introduced which is used for defining criteria of the absolute stability of the system (1). Conditions which parameters  $\tau_1 > 0, \tau_2 > 0, \theta$  and  $w(\omega)$  must satisfy that the solution  $X \in 0$  of system (1) be asymptotically stable in the large are presented in the form of two theorems. For the control system described by equations

$$dx/dt = Px + q\varphi(\sigma) + f(t, x); \quad \sigma = r^*x \quad (3)$$

where  $f(t, x)$  is a continuous function of  $x$  and  $t$  and

$$\lim_{|x| \rightarrow \infty} |f(t, x)| / |x|$$

converges toward zero uniformly with respect to  $t$ , and under the same assumptions as for system (1) except for condition (2a) which is replaced by a weaker one

$$\lim_{|\omega| \rightarrow \infty} \frac{1}{\omega} \left| \frac{w(\omega)}{X(\omega)} \right| > 0 \text{ at } |\omega| \rightarrow \infty.$$

where  $w(\omega)$  is a function which is established. If for certain parameters

... (x) there exists a bounded closed set F such that all of its elements

has ...

... integrability ... Leningrad State University

SUBMITTED: 26 Jun 64

ENCL ...

SUP CODE ... MA

NO ...

GROUP ...

ATT PRESS: 3182

Card 3/3



L 24596-66 EWT(d) IJP(c)

AGG NR: AP6009415

SOURCE CODE: UR/0020/66/166/006/1308/1311

28  
27  
B

AUTHOR: Yakubovich, V. A.

ORG: Leningrad State University im. A. A. Zhdanov (Leningradskiy gosudarstvennyy universitet)

TITLE: Recurrence finitely convergent algorithms for solving systems of inequalities

SOURCE: AN SSSR. Doklady, v. 166, no. 6, 1966, 1308-1311

TOPIC TAGS: algorithm, Euclidean space, Hilbert space, set theory, vector, real function

ABSTRACT: The infinite <sup>16</sup>system of inequalities

$$\varphi(x, a_j) > 0 \quad (j = 1, 2, \dots)$$

is examined, where  $x$  is the unknown vector of the euclidean or real Hilbert space  $R_1$ ;  $a_j$  are arbitrary vectors of some set  $M$  of a euclidean or real Hilbert space  $R_2$ ; and  $\varphi(x, a)$  is a real function. The derived algorithms have a number of common characteristics with relaxation algorithms. Besides being simple, they

2

Card 1/2

UDC: 519.95

L 24596-66

ACC NR: AP6009415

have high reliability. Five theorems are proved. Superposition of the algorithms  $x_j + 1 = f_j(x_j, c_j(x_j, a_j), Y_j(x_j, a_j))$  for  $x_1 \in G$  will be a finitely convergent algorithm for solution of the inequalities  $\Phi(x, a_j) > 0$ . Simple finitely convergent algorithms for solution of the inequalities  $\chi_j + 2(h_j, x) + (H_j, x, x) > 0$ , where  $H_j = H_j^* > 0$ , can be easily obtained by this method. "The author thanks V. I. Smirnov for a number of valuable comments." This paper was presented by V. I. Smirnov, academician, on 11 June 1965. Orig. art. has: 4 equations.

SUB CODE: 12/    SUBM DATE: 06Jun65/    ORIG REF: 005/    OTH REF: 004

Card 2/2 BK

L 27783-66 ENT(d)/T/ENP(1) IJP(c) GG/BB/JXT(CZ)

ACC NR: AP6012911

SOURCE CODE: UR/0020/66/167/005/1008/1011

AUTHOR: Kozinets, B. N.; Lantsman, R. M.; Yakubovich, V. A.

57  
56  
B

ORG: Lithuanian Scientific Research Institute for Forensic Examinations, Vilnius  
(Litovskiy Nauchno-Issledovatel'skiy institut sudebnoy ekspertizy)

TITLE: Criminalistic examination of similar handwriting by means of electronic computers

SOURCE: AN SSSR, Doklady, v. 167, no. 5, 1966, 1008-1011

TOPIC TAGS: computer application, adaptive pattern recognition, electronic computer, digital computer

ABSTRACT: One of the most difficult tasks in criminalistic examination is the identification of similar handwriting. The present authors developed a program for a learning digital computer which bases the recognition process on learning according to the algorithm which follows a training sequence. The graphical object is first converted into digital form by means of characteristic features. The processing of data is carried out by associating to the stereotype of the handwriting of a given person a sampling of convex sets. Computer recognition of true and forged signatures of the personnel of the Lithuanian Scientific Research Examinations (Litovskiy nauchno-issledovatel'skiy institut sudebnoy ekspertizy) was compared with the results of identifications by experts of the Leningrad Scientific Research Laboratory of Forensic Examinations (Leningradskaya nauchno-issledovatel'skaya laboratoriya sudebnoy ekspertizy), of the scientific technical department

Card 1/2

UDC: 519.95

L 27783-66

ACC NR: AP6012911

of the UM UOOPLO (nauchno-tehnicheskiy otdel), and the scientific-technical group of the highway department of the militia MOOP RSFSR (nauchno-tehnicheskaya gruppa dorozhnogo otdela militsii). Results are shown in Table 1.

Table 1 Handwriting recognition

Signature	Recognition, percent	
	Experts	Machine
Metsyavichyus	58.3; 68.3; 70	88
Shtromas	75.4; 78.9; 80.7	91.2
Chyapas	75.0; 80	84.2
Poshkyavichyus	90.0; 92	100

A more detailed account of the investigation will appear in Symposium No. 2 of the Lithuanian Scientific-Research Institute for Forensic Investigation which planned the study in conjunction with the Computer Center of Leningrad University (Vychislitel'nyy tsenter Leningradskogo universiteta). The authors express their gratitude to the experts of abovementioned institutions. The paper was presented by Academician Smirnov, V. I., 20 Jul 65. Orig. art. has: 1 table.

SUB CODE: 05, 09 / SUBM DATE: 17Jul64 / ORIG REF: 001

Card 2/2 CC

L 04900-67 EMT(d)/EWP(1) IJP(c) GG/BB/JXT(BF)/GD

ACC NRI AT6022670

SOURCE CODE: UR/0000/66/003/000/0021/0028

AUTHOR: Kozinets, B. N.; Lantsman, R. M.; Sokolov, B. M.; Yakubovich, V. A.

ORG: none

52  
B1

TITLE: Handwriting recognition and discrimination by means of electronic computers

SOURCE: Moscow. Institut avtomatiki i telemekhaniki. Samoobuchayushchiesya avtomaticheskkiye sistemy (Self-instructing automatic systems). Moscow, Izd-vo Nauka, 1966, 21-28

TOPIC TAGS: pattern recognition, automaton, character recognition, computer application

ABSTRACT: The general problem of machine recognition and discrimination of handwriting, the development of the necessary algorithms, and the theoretical principles underlying the process of teaching an automaton handwriting analysis are discussed. The discussion is based primarily on certain theoretical work in this area that has been carried out at the VTs LGU. A detailed explanation is given of the manner in which the handwriting or "graphic" material is converted into a system of numbers suitable for computer processing, and several different metrization techniques are described. The principle of the "dynamic stereotype of writing" (a fundamental assumption of the method proposed) is introduced as a means of neutralizing

Card 1/2

L 04900-67

ACC NR: AT6022670

random or deliberate handwriting deviations from an established and quantized standard. The necessary and sufficient conditions for the validity of this hypothesis are stated, and it is shown that algorithms based on this assumption are in all cases much simpler than those which disregard it. Examples are given and an analysis is made of the results of certain machine experiments using the general techniques outlined, including a comparison of the algorithm adopted with others founded on different approaches. The theoretical considerations and experiments described substantiate the possibility in principle of employing computers for the differentiation of similar handwriting styles. Orig. art. has: 8 figures.

SUB CODE: 09,06 / SUBM DATE: 02Mar66 / ORIG REF: 003

*ms*  
Card 2/2

L. 02/51-67 MPT(a) TJP(c)

ACC NR: AT6024067

SOURCE CODE: UR/2944/66/000/003/0051/0639

AUTHOR: Yakubovich, V. A. 14

ORG: none

TITLE: Regions of dynamic instability in Hamiltonian systems

SOURCE: Leningrad. Universitet. Kafedra vychislitel'noy matematiki i Vychislitel'nyy tsentr. Metody vychisleniy, no. 3, 1966, 51-59

TOPIC TAGS: linear differential equation, Hamilton equation, dynamic stability

ABSTRACT: The system studied is:  $J \frac{dx}{dt} = [C(\theta) + \epsilon H(t, \epsilon, \theta)] x. \quad (0.1)$ 

where  $x$  is a vector solution,  $J$  is a non-degenerate real skew-symmetric matrix, and matrices  $C$  and  $H$  are real-valued, symmetric for real  $\epsilon$ ,  $\theta$ , and depend analytically on the parameters in the region

$$-\infty < \theta_1 \leq 0 < \theta_2 < +\infty, |\epsilon| < \epsilon_0 < \infty. \quad (0.2)$$

A point of instability is defined as follows: a point  $(\epsilon_0, \theta_0)$  in region (0.2) is a point of instability if for  $\epsilon = \epsilon_0$ ,  $\theta = \theta_0$  equation (0.1) has solutions unbounded on  $(0, \infty)$ . Regions on the plane  $(\epsilon, \theta)$  into which an open set, obtained from the set  $M$  of all instable points by discarding boundary points, falls are called regions of dynamic

Card 1/2

L 09451-67

ACC NR: AT6024067

instability of equation (0.1). The value  $\theta_0$  is called critical for equation (0.1) if points of instability can be found arbitrarily close to the point  $(0, \theta_0)$ . The general form of such regions of instability is studied, and an algorithm is given for calculating the boundaries of regions of dynamic instability for small values of  $\epsilon$ . Orig. art. has: 76 formulas, 5 figures.

SUB CODE: 12/

SUBM DATE: 16Apr63/

ORIG REF: 011

Card 2/2



I. COMINT-67 EMT(a)/EPT(m)/EPP(w)/EPP(l) IJP(c) FM  
ACC TAG: AT6024069 SOURCE CODE: UR/2944/66/000/003/0076/0104

AUTHOR: Fomin, V. N.; Yakubovich, V. A. 2/1

ORG: none

TITLE: The computation of characteristic exponents for linear systems having periodic coefficients

SOURCE: Leningrad. Universitet. Kafedra vychislitel'noy matematiki i Vychislitel'nyy tseñtr. Metody vychisleniy, no. 3, 1966, 76-104

TOPIC TAGS: linear differential equation, dynamic stability, approximate solution

ABSTRACT: An equation is derived for determining the characteristic exponents of the system

$$\frac{dx}{dt} = [C + \epsilon D(t, \epsilon)] x,$$

For  $\epsilon = 0$ , they reduce to a given characteristic exponent  $\alpha_0$  of the unperturbed equation

$$\frac{dx}{dt} = Cx.$$

Formulas are also derived for the calculation by successive approximations of characteristic exponents for perturbed systems with periodic coefficients, for a vector equation of degree  $m$ , and for systems with multi-parametric perturbations. Some conclusions

Card 1/2

L 09441-67

ACC NR: AT6024069

are made concerning the effect of combinatory resonance on the stability of elastic systems. Orig. art. has: 175 formulas. 26 2

SUB CODE: 12/      SUBM. DATE: 16Apr63/      ORIG. REF: 011/      OTH REF: 006

Card 2/2

ACC NR: AP7001539

SOURCE CODE: UR/0020/66/171/003/0533/0536

AUTHOR: Yakubovich, V. A.

ORG: Leningrad State University im. A. A. Zhdanov (Leningradskiy gosudarstvennyy universitet)

TITLE: Periodic and nearly periodic limiting states of control systems with certain, generally speaking, discontinuous nonlinearities

SOURCE: AN SSSR. Doklady, v. 171, no. 3, 1966, 533-536

TOPIC TAGS: control system, automatic control system, system analysis, differential equation

ABSTRACT: Consider the differential equations of a control system with  $\kappa$  nonlinear units  $\varphi_j = \varphi_j(\sigma_j)$ 

$$\dot{x}/dt = Px + q\varphi(\sigma) + f(t), \quad \sigma = r^*x.$$

The matrices  $P, q, r, x, f(t), \varphi(\sigma) = \|\varphi_j(\sigma_j)\|$  are real and have respective orders  $v \times v, v \times \kappa, v \times \kappa, v \times 1, v \times 1, \kappa \times 1, \kappa \times 1$ , and  $\sigma = \|\sigma_j\|$  is  $\kappa \times 1$ . It is assumed that  $\varphi_j(\sigma_j)$  is a piecewise continuous function having only first-order points of discontinuity and that

$$0 \leq \Delta\varphi_j / \Delta\sigma_j \leq \mu_j, \quad j = 1, 2, \dots, \kappa,$$

where  $\Delta\varphi_j = \varphi_j(\sigma_j + \Delta\sigma_j) - \varphi_j(\sigma_j)$ ,  $-\infty < \sigma_j < +\infty$ ,  $-\infty < \Delta\sigma_j < +\infty$ , and  $\sigma_j, \sigma_j + \Delta\sigma_j$

Card 1/2

ACC NR: AP7001539

are points of discontinuity of the function  $\psi_j(\sigma_j)$ . Subject to other definitions and constraints, it is shown that the solution of this system is an arbitrary, absolutely continuous  $n \times 1$  matrix function  $x(t)$ . Then for a certain  $n \times 1$  matrix function  $\psi(t) = \|\psi_j(t)\|$ , (summed at each interval) and also for the function  $\varphi[\sigma(t)]$ , the relationship  $dx/dt = Px + \bar{q}\psi(t) + f(t)$ ,  $\varphi_j[\sigma_j(t) - 0] \leq \psi_j(t) \leq \varphi_j[\sigma_j(t) + 0]$ , where  $\sigma(t) = \|\sigma_j(t)\| = r \cdot \dot{x}(t)$ , is nearly always satisfied. Four theorems are stated and proved in demonstration of the existence of an exponential convergence of the system solution. Parts of the proof were presented by the author in an earlier paper (Avtomatika k telemekh., 25, No. 7, 1964). This paper was presented by Academician L. S. Pontryagin on 24 January 1966. Orig. art. has: 5 equations.

SUB CODE: 12/<sup>13</sup> SUBM DATE: 24Jan66/ ORIG REF: 006/ OTH REF: 004

Card 2/2

ACC NR: AT6022669

SOURCE CODE: UR/0000/66/000/000/0009/0020

AUTHOR: Yakubovich, V. A.

ORG: none

TITLE: Some basic principles of the design of cognitive learning systems

SOURCE: Moscow. Institut avtomatiki i telemekhaniki, Samoobuchayushchiesya avtomaticheskiye sistemy (Self-instructing automatic systems). Moscow, Izd-vo Nauka, 1966, 9-20

TOPIC TAGS: intelligent machine, speech recognition, pattern recognition, character recognition, adaptive pattern recognition, sound recognition computer, artificial intelligence

ABSTRACT: The author describes a mathematical basis for the development of learning, pattern recognition machines. In addition, the results of certain experiments carried out using a machine constructed in accordance with the proposed theory are reported. A learning machine functions by association of the stimulæ presented with previously acquired and stored information. The training process therefore consists of feeding into the machine the inputs to be recognized, as well as the corresponding correct outputs (responses). The amount of required information can be substantially reduced and performance improved by giving the machine the ability to recognize the inputs by

Card 1/2

ACC NR: AT6022669

classifying them as belonging to a set of similar, familiar inputs. An input can be considered in mathematical terms to be a set  $S$ . This set can have certain general properties which can be used for its classification as a preliminary to its recognition. The set  $S$  may be open, connected, and in many cases, convex. The author does not postulate that biological systems function in accordance with this principle; he suggests, however, that during the process of evolution, living organisms sensed and utilized the general properties of sets. Consequently, the proposed method appears reasonable. A mathematical basis for systems designed to differentiate between various types of convex and non-convex sets is given and related to some olfactory, auditory, and visual stimulæ. An artificial retina of  $10 \times 10$  cm was constructed and operated in conjunction with a computer. The inputs were in terms of coordinates for 25 points of an image. The experiment of recognition of handwritten numbers consisted in presenting the retina with five numbers "2" and five numbers "3". All numbers were different in shape, size, and their location on the retina. This constituted the training phase. Thereafter fourteen images (seven "two's" and seven "three's") were presented, of which the machine correctly identified twelve. The experiment of human profile recognition had the criterion of classifying a profile either as an "up-turned nose" or as a "long nose". After an initial training phase the machine correctly recognized all forty-two profile images presented. Two other experiments dealing with recognition of sounds and random terms are also described. The sounds were translated into curves of spectral densities and presented to the retina. The author expresses his gratitude to Prof. G. V. Gershuni and Prof. L. A. Chistovich for the use of spectral density recordings. Orig. art. has: 11 figures.

SUB CODE: 06,05/ SUBM DATE: 02Mar66/ ORIG REF: 007/ OTH REF: 004

Card 2/2

ARTEMOV, Yu.V.; KOZINETS, B.N.; YAKUBOVICH, V.A.

Effect of impact on a multimass system. Metod. vych. no.2:75-90  
'63. (MIRA 18:11)

YAKUBOVICH, V.A.

Teaching a machine to perceive an image. Metod. vych.  
no.2:95-131 '63. (MIRA 18:11)



L 00592-66

ACCESSION NR: AR5019350

UR/0124/65/000/007/A011/A012  
531.36+531.391.3

SOURCE: Ref. zh. Mekhanika, Abs. 7A97

AUTHOR: Yakubovich, V. A.; Starzhinskiy, V. M.

TITLE: A parametric resonance system with multiple degrees of freedom

CITED SOURCE: Tr. Mezhvuz. konferentsii po prikl. teorii ustoychivosti dvizheniya i analit. mekhan., 1962. Kazan', 1964, 123-134

TOPIC TAGS: canonic equation system, frequency order, forced oscillation stability, resonant system, instability area boundary

TRANSLATION: The authors analyze the equation system  $\frac{dx}{dt} = [C + \epsilon A(\vartheta t)] x$  where C is a constant  $2k \times 2k$  matrix with pure imaginary eigenvalues  $j\omega, (\nu = \pm 1, \dots, \pm k)$ .

Card 1/2

L 00592-66

ACCESSION NR: AR5019350

while  $A(s)$  is a  $2 \times 2$  periodic matrix. All critical frequencies are given for some classes (i. e.  $t$ -invariant, canonical) of systems of type (1). These assume the form

$$\omega_0 = |\omega_j \pm \omega_h|/m \quad (j, h = \pm 1, \dots, \pm h, m = 1, 2, \dots)$$

A formulation of the M. G. Krein theorem for canonic systems is presented, employing the concepts of first and second order frequencies. Formulas are given for canonic equation systems to define boundaries of instability areas in plane  $\mathcal{E}$  with an accuracy ranging to small  $O(\epsilon)$  inclusive. The importance of a study of combination resonances in system (1) are emphasized and the feasibility of expanding combination resonance regions by introducing minor friction is indicated. Calculation results are cited to clarify the failure of the Takomskiy bridge. Formulas are given for first approximations of characteristic exponents of systems similar to canonic. The results derived are applied in a study of the stability of forced periodic oscillations in the quasilinear system

$$M\ddot{u} + Q_0\dot{u} + P_0u = f(t) + \epsilon g(t, u, \dot{u}, \epsilon) \\ f(t+T) = f(t), \quad g(t+T, u, \dot{u}, \epsilon) = g(t, u, \dot{u}, \epsilon)$$

for resonant and nonresonant formulations. K. G. Valeyev

SUB CODE: ME, MA

ENCL: 00

Card 2/2 DP

YAKUBOVICH, V.M., inzh.; YASINOVSKIY, L.L., inzh.

Enrichment of limestone in the DEK-20 classifier. Stroi. mat. li no.6:  
35-36 Je '65. (MIRA 18:7)

LUTKOVSKAYA, T.A.; SOKRATOV, G.I.; YAKUBOVICH, V.S.

Sedimentary and volcanic sedimentary formations, intrusive complexes, and metallogenetic zones in the southwestern part of the Zaysan geosyncline. Trudy VSEGEI 103:59-83 '64 (MIRA 17:8)