

MARKOV, A. A.

*Be*

3478. Impulsive potential on a resistive and capacitive load. A. A. MARKOV. *Zh. tekhn. Fiz.*, 23, No. 11, 2071-74 (1955) in Russian.

A series of general observations are made on the form and amplitude of the potential across a parallel resistance-capacitance combination for various impulse currents. These observations are shown to apply for a similar RC network whose circuit is given. The potential is examined for exponential current impulses and curves are given showing variation of amplitude with resistance for several forms of this impulse.

V. V. ZAKHAROV

*Be*

MARKOV, A. A.

621.373.43 : 621.3.018.75

4716. The nature of the influence of loading on the form of a voltage impulse. A. A. MARKOV. *Zh. eksper. teor. Fiz.*, 24, No. 2, 214-216 (1953), in Russian.

The source is a generator of unit-function constant current. The load circuits are either a parallel-connected resistor and capacitor or circuits which are reducible to this form. The operational solution of the network equations is explained, and it is shown that the effect of a series capacitor between the source and load is to lengthen the voltage pulse in comparison with the current pulse.

S. C. DUNN

B7

MARKOV A.A.

1 - RMZ

Measurement of the lifetime of  $\pi^+$  mesons. M. S. Kozhdaev, A. A. Markov, and A. A. Tyapkin. *Bull. Acad. Sci. U.S.S.R., Phys. Ser.* 6, 647-51 (1965) (English translation). — See C.A. 50, 7018a. B. M. R.

RMZ  
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MARKOV, A.A.

Type GIM-4 pulse generator. Sbor.hauch.rab. MIFI no.9:135-144 '55.  
(MIRA 10:1)

(Pulse techniques (Electronics))

GAYDAYEV, G.L.; MARKOV, A.A.; TSAREGRODTSEV, M.N.

Device for recording out-of-phase (inhibited) coincidences, Shgr.  
nauch.rab. MIFI no.9:145-154 '55. (MIRA 10:1)  
(Pulse techniques (Electronics))

Markov, A.A.

109 RMJ

Formation of neutral mesons by high-energy nucleons.  
M. S. Korodkov, A. A. Tyapkin, Yu. D. Bayukov, A. A.  
Markov, and Yu. D. Prokoshkin. *Bull. Acad. Sci.*  
*USSR Phys. 10, 629-33 (1965) (Engl. translation). - See C.A.*  
*150, 7010c.* H.M.R.

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KLS

KOZODAYEV, M.S.; TYAPKIN, A.A.; BAYUKOV, Yu.D.; MARKOV, A.A.; PROKOSHKIN, Yu.D.

Production of neutral mesons by high-energy nucleons. Izv. AN SSSR. Ser. fiz. 19 no. 5:589-603 S-O '55. (MLRA 9:4)

1. Institut yadernykh problem Akademii nauk SSSR.  
(Cosmic rays) (Nuclear physics)

KOZODAYEV, M.S.; MARKOV, A.A.; TYAPKIN, A.A.

Measuring  $\pi^+$ -meson lifetime. Izv.AN SSSR.Ser.fiz.19 no.6:  
715-719 N-D '55. (MLRA 9:4)

1.Institut yadernykh problem Akademii nauk SSSR.  
(Cosmic rays) (Nuclear physics)



Maerkov, A. A.

USSR

✓ 8481 AEO-17-3179  
HYPERONS AS EXCITED STATES OF NUCLEONS. A  
POSSIBLE MECHANISM OF MULTIPLE FORMATION OF  
PARTICLES. A. A. Maerkov. Translated from Doklady  
Akad. Nauk S.S.S.R. 151, 400-39(1963). Cp.

MIRKOV, A. A.

"Inversion of Complicated Systems of Functions."

report presented at All-Union Conference in Problems in the Theory of Relay Devices,  
Inst. for Automation and Remote Control AN USSR, 3-9 Oct 1957.  
Vestnik AN SSSR, 1958, No. 1, v. 28, pp. 131-132. (author Ostianu, V. M.)

MARCOV, A. A.

"Errors in Orientations of Filtrating Irradiation," paper presented at the  
4th International Electronics and Nuclear Energy Exhibition and Conference in  
Rome, ~~Italy~~ Italy, 22 Jun-6 Jul 1957

d-3, 000, 612, 25 Oct 57

*MORRIS*

1-1-60

APPROX:  $\frac{1}{n} \sum_{i=1}^n x_i$ , A.A.

... (i) ...

... (1950)

... (1950)

$$s = (x - \bar{x})/n \approx \dots$$

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2/2 1. Pulse counters-Errors 2. Mathematical-Theory

BOV-120-53-3-33/33

AUTHORS: Makrov, A. A. and Sofiyev, G. N.

TITLE: *What should be the Design of a Pulse-Generator for Work with Amplitude Analysers (Kakim dolzhen byt' seriyanyy generator impul'sov dlya raboty s amplitudnyimi analizatorami)*

PERIODICAL: Priborny i Tekhnika Eksperimenta 1957, No. 8, pp. 10-11 (USSR)

ABSTRACT: A specification is given for a generator suitable for work with amplitude analysers. The specification is a list of 31 items and a block diagram (Fig.1). There is 1 figure, no tables and no references.

SUBMITTED: September 2, 1957.

1. Pulse generators--Design 2. Pulse generators--Specifications

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SOV/120-58-6-4/32

AUTHORS: Bayukov, Yu. D., Kozodayev, M. S., Markov, A. A., Sinayev, A. N., Tyapkin, A. A.

TITLE: A Multichannel Pair  $\gamma$ -Spectrometer. I. Calculation of the Main Characteristics of the  $\gamma$ -Spectrometer (Mnogokanal nyy parnyy gamma-spektrometr. I Raschet osnovnykh kharakteristik gamma-spektrometra)

PERIODICAL: Pribory i tekhnika eksperimenta, 1958, Nr 6 pp 23-29 (USSR)

ABSTRACT: In a pair  $\gamma$ -spectrometer the energy of the quanta is determined by measuring the total energy of the components of the electron-positron pair formed in a thin converter. The first 2-channel pair spectrometer was built by Dzhelepov (Ref. 1). Later spectrometers built on this principle were widely used in measuring the spectra of hard  $\gamma$ -rays (Refs. 2 to 8). The electron and the positron leaving the converter were deflected by a magnetic field in different directions and for certain values of their energy they enter ionisation counters connected in coincidence. For a given intensity of the magnetic field and a fixed position of the counters such a spectrometer will record a fraction of the pairs produced by  $\gamma$ -rays in a given energy range. In a simple 2-channel spectrometer in which one channel records the electrons and

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SOV/120-58-6-4/32

A Multichannel Pair  $\gamma$ -spectrometer. I Calculation of the Main Characteristics of the  $\gamma$ -spectrometer

the other the positrons, an increase in the accuracy of measurement is associated with a marked decrease in the efficiency. Good energy resolution and high efficiency can only be simultaneously achieved in a multichannel spectrometer. In such a spectrometer the efficiency may be increased by a factor  $n_2$  without loss of resolution where  $n_1$  and  $n_2$  are the numbers of electron and positron counters, respectively. In such a spectrometer several energy intervals may be analyzed at the same time. A number of such multichannel spectrometers have been described (Refs. 5, 6 and 8). The characteristics of a  $\gamma$ -spectrometer as a measuring instrument is determined by its efficiency and spectral sensitivity. In a multichannel system it is necessary to take into account the characteristics for the various pairs of channels of the spectrum. In this connection, a discussion is given in the present paper of the dependence of the efficiency and spectral sensitivity of the separate pairs of channels on various

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SOV/120-58-6-4/32

A Multichannel Pair  $\gamma$ -spectrometer. I. Calculation of the Main Characteristics of the  $\gamma$ -spectrometer

parameters of the spectrometer:

1) Spectral sensitivity: the basic diagram of a  $\gamma$ -spectrometer considered in this paper is shown in Fig.1, in which the meanings of the symbols employed are indicated. In view of the finite width of the counters, the spectrometer records  $\gamma$ -quanta in a certain energy interval from  $E_{\gamma \text{ min}}$  to

$E_{\gamma \text{ max}}$ . The corresponding spectral sensitivity curve is then shown in Fig.2a and is of triangular form with a dispersion given by

$$\sigma_{12} = 1/6 \ell_c^2 / (r_1 + r_2)^2 \quad \text{where } \ell_c \text{ is the width of a}$$

counter and  $r_1$  and  $r_2$  are the distances from the converter to the centres of the counters, respectively. The effect of the width of the converter upon the spectral sensitivity is examined and it is shown that a converter of a finite width introduces a spread into the spectral line in the high energy region of  $\gamma$ -quanta. As the angle  $\varphi$  between the direction of motion of the  $\gamma$ -quanta and the

Card 3/6 straight line connecting the centre of the converter with

SOV/120-58-6-4/32

A Multichannel Pair  $\gamma$ -spectrometer. I. Calculation of the Main Characteristics of the  $\gamma$ -spectrometer

the counter increases, the spread of the spectral line decreases. At  $\varphi = 90^\circ$  the width of the spectral sensitivity curve is independent of the converter width. The effect of the converter width gives a distribution of the form shown in Fig.2b, which has a dispersion given by:

$$\sigma_2^2 = \frac{L_k^4 \text{ctg}^4 \varphi}{180r_1^2 r_2^2} \quad . \quad \text{The effect of multiple}$$

scattering in the converter is estimated and expressions are derived for this effect also. Finally, an estimate is given for the radiation loss experienced by the electron-positron pair on traversing the converter.

2) Efficiency: in this section the Bethe-Heitler expression for the probability of formation of a pair by a  $\gamma$ -quantum of

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SOV/120-53-6-4/32

A Multichannel Pair  $\gamma$ -spectrometer. I. Calculation of the Main Characteristics of the  $\gamma$ -spectrometer

energy  $E_\gamma$  is used (Ref. 13) with a modification described by Bethe  $\gamma$  et al in Ref. 22.

3) Multichannel system: in a multichannel spectrometer the electrons and positrons formed by  $\gamma$ -quanta of a given energy are recorded by a number of combinations of pairs of counters. The electronic circuit of such a spectrometer should record coincidences between pulses from each electron counter with pulses from any positron counter. Thus, any combination of one electron counter and one positron counter is, in fact, a 2-channel spectrometer. For a given geometry a spectrometer containing  $n$  channels records  $\gamma$ -quanta in  $n-1$  energy intervals of different mean energy. In practice, one seeks to find the form of the spectrum and the absolute intensity in one of the energy intervals. To find the form of the spectrum it is sufficient to know the relative efficiency of recording for the different energy intervals, and this is given by Eq. (10). In order to obtain the absolute intensity in one of the energy intervals it is necessary to know the total absolute efficiency of recording of  $\gamma$ -quanta in one of the energy intervals. This problem is not treated.

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SOV/120-58-6-4/32

A Multichannel Pair  $\gamma$ -spectrometer. I. Calculation of the Main Characteristics of the  $\gamma$ -spectrometer

V. V. Mel'nikov is thanked for carrying out a number of calculations. There are 2 figures and 22 references of which 4 are Soviet, 1 German, 1 Soviet translated from English and the rest are English.

ASSOCIATION: Ob'yedinenyye Institut yadernykh issledovaniy (United Institute for Nuclear Studies)

SUBMITTED: December 27 1957

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SOV/120-58-6-5/32

AUTHORS: Bayukov, Yu. D., Kozodayev, M. S., Markov, A. A. Sinayev A Tyapkin, A. A.

TITLE: A Multichannel Pair  $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer (Mnogokanal'nyy parnyy gamma-spektrometr. II. Opisaniye dvenadtsatikanal'nogo spektrometra)

PERIODICAL: Pribory i tekhnika eksperimenta, 1958, Nr 6. pp 30-40 (USSR)

ABSTRACT: Application of a multichannel pair spectrometer in synchro-cyclotron work presents a number of specific requirements as far as counters of the ionising particles and the electronic system of the spectrometer are concerned. Since the beam intensity is high and consists of short pulses of 200 to 300  $\mu$ s each at a repetition frequency of 40 to 80 pulses per sec, it follows that the apparatus must be very fast. It is desirable that the input blocks should have resolving times not greater than 1  $\mu$ s. The large background intensity in synchro-cyclotron work means that it is always necessary to use a special selection system which records only electron-positron pairs. For this reason, in the spectrometer each component of a pair should be recorded by a number of counters in coincidence with sufficiently low resolving time. The Card 1/7 present paper describes a 12-channel  $\gamma$ -spectrometer which has

SOV/120-58-6-5/32

## A Multichannel Pair $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer

been used over a number of years in studying the spectra of hard  $\gamma$ -rays and neutral  $\pi$ -meson decays (Refs.2-6). The first variant of the spectrometer was built in 1947. In 1953 and 1954 the spectrometer was modified to improve its characteristics. The spectrometer described here satisfies completely the above requirements and is based on the design calculations given in the previous paper (Ref.1) in this issue.

### 1) Magnetic system and geometry of the instrument

The magnetic field is produced by an SP-56 electromagnetic. Fig.1 shows the disposition of the counters for two types of demountable pole pieces. The gap between the poles is 18 cm and the maximum field in the gap is 18 000 oersted. The electromagnet current is stabilised to 0.1%. In studies of  $\gamma$ -ray spectra in the energy region 20 to 200 MeV,  $2\phi = 180^\circ$  (Fig.1b) and in the energy region 100 to 450 MeV,  $2\phi = 90^\circ$  (Fig.1a). In the former case semi-circular focussing of

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A Multichannel Pair  $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer

electrons and positrons was used, and this led to increased efficiency (Ref.1) because it was possible to use wider and thicker converters. For  $\gamma$ -quanta in the energy range 450-600 MeV,  $2\phi = 90^\circ$  but the counters were at a larger distance from the converter. Copper converters were used (0.1, 0.3 and 0.5 mm, depending on the energy).

2) Resolving power and efficiency.

Fig.2 shows curves of the total spectral sensitivity for the 7th energy interval for various values of  $E_{\gamma 0}$  and thicknesses  $T_k$  of the copper converters. These curves are based on the theoretical data given in the previous paper and are obtained by a statistical combination of the partial distributions due to a) width of the counters, b) width of the converter, c) multiple scattering and d) radiation. As can be seen, the form of the total spectral sensitivity curve is **very** nearly triangular, which means that the total spectral sensitivity is governed mainly by the width of the channels  $\ell_c$  (see Fig.1 of previous paper, p 24, this issue).

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A Multichannel Pair  $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer

3) Counters and selection system. The counters used were proportional counters having a cylindrical stainless steel cathode, 10 mm in diameter and a molybdenum filament 0.1 mm in diameter. They were filled with  $(\text{CH}_2(\text{OCH}_3)_2)$  at a pressure of 160 to 200 mm. The working voltage was 1600 to 2000 V. The counters have an effective dead time not exceeding  $10^{-7}$  sec. The efficiency of the counters for particles with relativistic ionisation reaches 98% in a coincidence scheme with a resolving time of  $5 \times 10^{-7}$  sec. The delay of the pulses due to drift of electrons through the counter gas is less than  $10^{-7}$ . The counters give electrical pulses with amplitudes between  $10^{-4}$  and 1 V. The large difference in the amplitudes requires the use of amplifiers having a wide dynamic range and an amplification of a few thousands. 6-fold coincidences were used and the number of random coincidences in each 6-fold channel was 0.02 pulses per sec. The number of electron-positron pairs recorded per

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A Multichannel Pair  $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer

sec depended on the efficiency of the spectrometer with respect to the  $\gamma$ -quanta in the measured energy interval and the form of the spectrum and was in the range 0.1 to 10 pair per sec.

4) Electronic scheme.

A block diagram of the electronic part of the spectrometer is shown in Fig.3. The left-hand portion of this diagram shows 6 co-ordinate counters of the electron series ( $a_1 - a_6$ ), 6 co-ordinate counters of the positron series ( $\bar{b}_1 - \bar{b}_6$ ) and 4 selection counters ( $A', A'', \bar{b}'$  and  $\bar{b}''$ ). Each of these counters in practice consists of a group of counters whose filaments are connected. A recorded electron or positron should pass through 3 counters (1 co-ordinate and 2 selection counters). A pair is recorded if a 6-fold coincidence takes place. Negative-going pulses from each counter are amplified by a corresponding amplifier-converter (Fig.4). These amplifiers have a rise time of  $2 \times 10^{-4}$  sec. Pulses from all the 16 amplifier-converters are applied to the main block which is at a distance of 1.5 m from the amplifier-converter (Fig.5). Pulses from the selection counters are applied to

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A Multichannel Pair  $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer

4-fold coincidence scheme while pulses from the co-ordinate counters are applied to mixers and in addition through delay lines to a hodoscopic system consisting of 2-fold coincidence circuits and output univibrators. The pulse at the output of a mixer appears in the presence of a pulse in at least one of the co-ordinate counters of a given series. Pulses from both the mixers and also from the 4-fold coincidence scheme are applied to a 3-fold coincidence scheme which produces the final output pulse. It follows that the latter pulse appears when a 6-fold coincidence takes place, i.e. when a particle passes through at least one of the co-ordinate counters in the electron series, through one of the co-ordinate counters of the positron series, and all the counters of the selective system. The resolving time of the above coincidence schemes is  $5 \times 10^{-7}$ .

5) Method of measurement and treatment of results.

Fig.7 shows the experimental arrangement. In this figure 1 is the proton trajectory, 2 is the target, 3 is the synchrocyclotron chamber, 4 is a concrete wall, 5 is a collimator.

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A Multichannel Pair  $\gamma$ -Spectrometer. II. Description of a 12-channel Spectrometer

6 is a diaphragm, 7 is a clearing magnet which removes electrons and positrons from the beam, 8 is an additional screen, 9 is the convertor and 10 is the spectrometer electro magnet. Fig.8 shows a typical result obtained for the energy spectrum of  $\gamma$ -quanta from neutral  $\pi$ -meson decays. The mesons were produced by 660 MeV protons at a carbon target. The spectra are measured at an angle of  $180-0^\circ$  to the direction of motion of the protons. G.P.Zorin, B.A.Krasnovidov, L.A.Fadeyev and G.N.Stepanov are thanked for their assistance. There are 8 figures, 4 tables and 7 Soviet references.

ASSOCIATION: Ob'yedinenny institut yadernykh issledovaniy (United Institute for Nuclear Studies)

SUBMITTED: December 27, 1957.

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SOV/120-59-1-38/50

AUTHOR: Markov, A. A.

TITLE: A Method for the Measurement of the Ratio of Pulse Heights  
(Metod izmereniya otnosheniya amplitud impul'sov)

PERIODICAL: Pribory i tekhnika eksperimenta, 1959, Nr 1, p 158 (USSR)

ABSTRACT: In experimental nuclear physics it is sometimes necessary to measure the ratio of pulse heights of coincident pulses. This problem may be solved by means of the apparatus shown diagrammatically in Fig 1. Short pulses whose heights are  $u_a$  and  $u_b$  are applied to the two inputs and the condensers  $C_a$  and  $C_b$  are charged to roughly the same values through the two diodes and then begin to discharge through  $R_a$  and  $R_b$ . Assuming that  $R_a C_a$  and  $R_b C_b$  are both equal to  $\tau$  and that the latter time constant is much greater than the pulse length one finds that the voltages across the condensers will fall off exponentially with a time constant equal to  $\tau$ . These voltages are applied to two pulse height discriminators with the same threshold  $E$ . The voltages across the condensers will be equal to the threshold voltage at different times

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A Method for the Measurement of the Ratio of Pulse Heights

$t_a$  and  $t_b$  so that

$$E = u_a \exp\left(-\frac{t_a}{RC}\right) = u_b \exp\left(-\frac{t_b}{RC}\right)$$

This is illustrated in Fig 2. The difference between the times when the voltages are across the two condensers become equal to the threshold of the discriminators is then given by

$$t_a - t_b = RC \log(u_a/u_b) .$$

It follows that the logarithm of the ratio of the pulse heights is proportional to the time difference and thus may be determined using one of the well-known time interval analyzers. The method was suggested in 1956 and was reported

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30V/120-59-1-38/50

A Method for the Measurement of the Ratio of Pulse Heights  
at the All-Union Conference on Analyzers in 1957. There are  
2 figures.

SUBMITTED: January 31, 1956.

Card 3/3

24 (4), 21 (8)

AUTHORS:

Vasil'yev, G. Ya., Usatyi, A. F.,  
Lazurkin, Yu. S., Markov, A. A.

SCV/20-125-6-11/61

TITLE:

Measurement of the Luminescence and Darkening of Glass During  
the Process of Their Irradiation in a Nuclear Reactor  
(Izmereniye lyuminestsentsii i potemneniya stekol v protsesse  
ikh oblucheniya v yadernom reaktore)

PERIODICAL:

Doklady Akademii nauk SSSR, 1959, Vol. 125, Nr. 6,  
pp 1219-1222 (USSR)

ABSTRACT:

The present paper is intended to work out the construction of  
device for the simultaneous measurement of the luminescence  
and darkening of transparent materials in a nuclear reactor  
and to deal with the carrying out of experiments by means of  
this apparatus. The usefulness of parallel measurements of  
the yield of the luminescence and of the darkening of the  
sample may be seen from the close connection between these  
phenomena during irradiation. The device consists of an  
aluminum tube of 5 m length and 60 mm diameter, inside of  
which two tubes of the darkening tract (polished inside) and  
one polished tube of the luminescence tract were fitted.  
Further details of the apparatus are described. Luminescence

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Measurement of the Luminescence and Darkening of SCV/20-125-6-11/61  
Glass During the Process of Their Irradiation in a Nuclear Reactor

and darkening were measured in the perpendicular, dry, channel of 65 mm (with external water-cooling) of the experimental reactor VVR. In this reactor ordinary water is used as moderator and coolant. The channel was near the active zone of the reactor. By variation of the power of the reactor various values are obtained for the differential dose. In the case of all experiments temperature remained below 35°. The samples consisted of 10 mm thick disks with a diameter of 20 mm. The following quantities were measured by remote control:

- the brightness of luminescence and its time dependence at various differential doses.
- The darkening of the samples and their time dependence at various differential doses.
- Measurement of darkening after irradiation was stopped.

Measurements were carried out on various types of quartz, pyrex glass, cerium glass, polymethylmethacrylate, and polystyrene. In the case of all quartz samples, the relation  $B = \beta P$  holds up to a differential dose of  $P = 2000$  rad/sec, where  $\beta$  denotes the specific brightness coefficient of luminescence. In the case of polymethylmethacrylate and polystyrene the brightness of luminescence increases with progress in

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Measurement of the Luminescence and Darkening of SOV/20-125-6-11/61  
Glass During the Process of Their Irradiation in a Nuclear Reactor

time and increasing integral dose. The optical density D for some dozens of minutes remains on the equilibrium level, the amount of which depends on the differential dose, and changes only little with an increase of the integral dose. The measurements carried out in the course of this investigation are only the first part of a series of measurements which is planned. There are 3 figures and 2 Soviet references

PRESENTED: January 8, 1959, by A. P. Aleksandrov, Academician

SUBMITTED: September 23, 1958

Card 3/3

MARKOV, A. A., DYAKOV Yu. Ye., SAKALYAN, K., and SHEBESHTEN, B.

"Impulse Scaling Circuit Using new System with Multiple Equilibrium States"

Joint Institute of Nuclear Research, Dubna, USSR.

report submitted for the IAEA conf. on Nuclear Electronics. Belgrade, Yugoslavia  
15-20 May 1961

S/120/62/000/003/004/048  
2032/E114

AUTHOR: Markov, A.A.

TITLE: Difference measurements in multichannel spectrometers

PERIODICAL: Pribory i tekhnika eksperimenta, no.3, 1962, 30-35

TEXT: It is pointed out that low-intensity photopeaks at low energies may become masked by the Compton distributions belonging to higher energy photopeaks. Such photopeaks can be separated by subtracting from the overall spectrum the high-energy components. The present author gives a general description of a procedure whereby this may be done (semi-automatically) in practice. Thus, once the main peaks in the spectrum under investigation have been identified, pure sources are introduced in place of the specimen under investigation and their spectra subtracted from the original spectrum. Background and statistical errors must be taken into account in such procedures and the author gives a general analysis of them. The discussion is concerned both with amplitude analysers and time selectors. No experimental results are reported.

SUBMITTED: June 15, 1961

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S/120/62/000/006/019/029  
E140/E435

AUTHORS: Levin, G.L., Markov, A.A., Plakhov, A.G., Smolkin, G.Y.  
Sofiyev, G.N., Stepanov, G.N., Shapkin, V.V.

TITLE: Line and frame scanning generator for electron-optical  
image intensifiers

PERIODICAL: Pribory i tekhnika eksperimenta, no.6, 1962, 100-106

TEXT: The authors discuss the use of image-intensifier tubes for  
the spectroscopic and space-geometric study of pulsed gas  
discharges in plasma studies (controlled thermonuclear synthesis).  
The system permits spectral analysis of dynamic processes with  
time resolution in the range  $5 \times 10^{-8}$  to  $1.25 \times 10^{-5}$  sec.  
A five-stage intensifier is used. Free-running and triggered  
versions are used, the latter to reduce background noise where  
necessary. There are 6 figures.

ASSOCIATION: Institut atomnoy energii AN SSSR  
(Institute of Atomic Energy AS USSR)

SUBMITTED: January 25, 1962  
Card 1/1

MARKOV, A.A.

Difference measurements in multichannel spectrometers. Prib. i  
tekh. eksp. 7 no.3:30-35 My-Je '62. (MIRA 10:7)  
(Optical measurements) (Spectrometer)

L 35349-66 EWT(m)

ACC NR: AR6017791

SOURCE CODE: UR/0058/66/000/001/A044/A04

AUTHOR: Markov, A. A.

24  
B

TITLE: Coincidences of arbitrary multiplicity

SOURCE: Ref. zh. Fizika, Abs. 1A397

REF SOURCE: Tr. 6-y Nauchno-tekhn. konferentsii po yadern. radioelektron. T. 2. M., Atomizdat, 1965, 42-51

TOPIC TAGS: coincidence circuit, nuclear radiation, radiation measurement

ABSTRACT: The author considers one case that is frequently encountered in the practice of measurement of nuclear radiation when it is necessary to register coincidences of arbitrary multiplicity from several (m) pickups. In this case all the signals entering the m inputs must be divided into two groups: a) noncoinciding and b) coinciding, for at least two arbitrary inputs. Depending on the purpose of the system, it is necessary to ensure in its measurement of either only such signals when an arbitrary coincidence took place, or, to the contrary, signals which do not coincide. Several practical examples of measurement of nuclear radiation are presented, in which it is necessary to have such a coincidence registration system. Different methods of construction of such systems are analyzed. A method of constructing a system of this type, which appears to be the simplest, is described. M. L. [Translation of abstract]

SUB CODE: 18, 09

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*Ed*

L 34797-66 FWT(d)/EWP(1) IJF(c) BB/GG

ACC NR: AR6017207

SOURCE CODE: UR/0058/65/000/012/A034/A034

AUTHOR: Markov, A. A.

TITLE: Calibration and stabilization of slope and shift of an amplitude characteristic

SOURCE: Ref. zh. Fizika, Abn. 12A323

REF SOURCE: Tr. 6-y Nauchno-tekhn. konferentsii po yadern. radioelektron. T. 1. M., Atomizdat, 1964, 81-89

TOPIC TAGS: coding, pulse amplitude, pulse amplifier, pulse height analyzer, automatic stabilization equipment

ABSTRACT: Methods are considered for calibrating and stabilizing the slope and shift of the amplitude characteristic of converters of an input quantity into a unitary code. It is noted that the gain calibration error of a proportional amplifier can be decreased by determining the gain from the measured ratio of increments of the input and output quantities. To stabilize the gain, it is proposed to apply to an auxiliary control input of the amplifier an error-signal voltage equal to the difference between the actual pulse amplitude and a standard signal converted from a pulse into a slowly varying voltage. In the case of a linear pulse-height discriminator with a characteristic shifted relative to zero, the stabilization of the shift can also be attained by means of a circuit that compares the output voltage pulse with a reference voltage. The slope of the characteristic can be stabilized with a cir-

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cuit that compares the difference of two output signals. Corresponding calculation formulas are presented. G. K. [Translation of abstract]

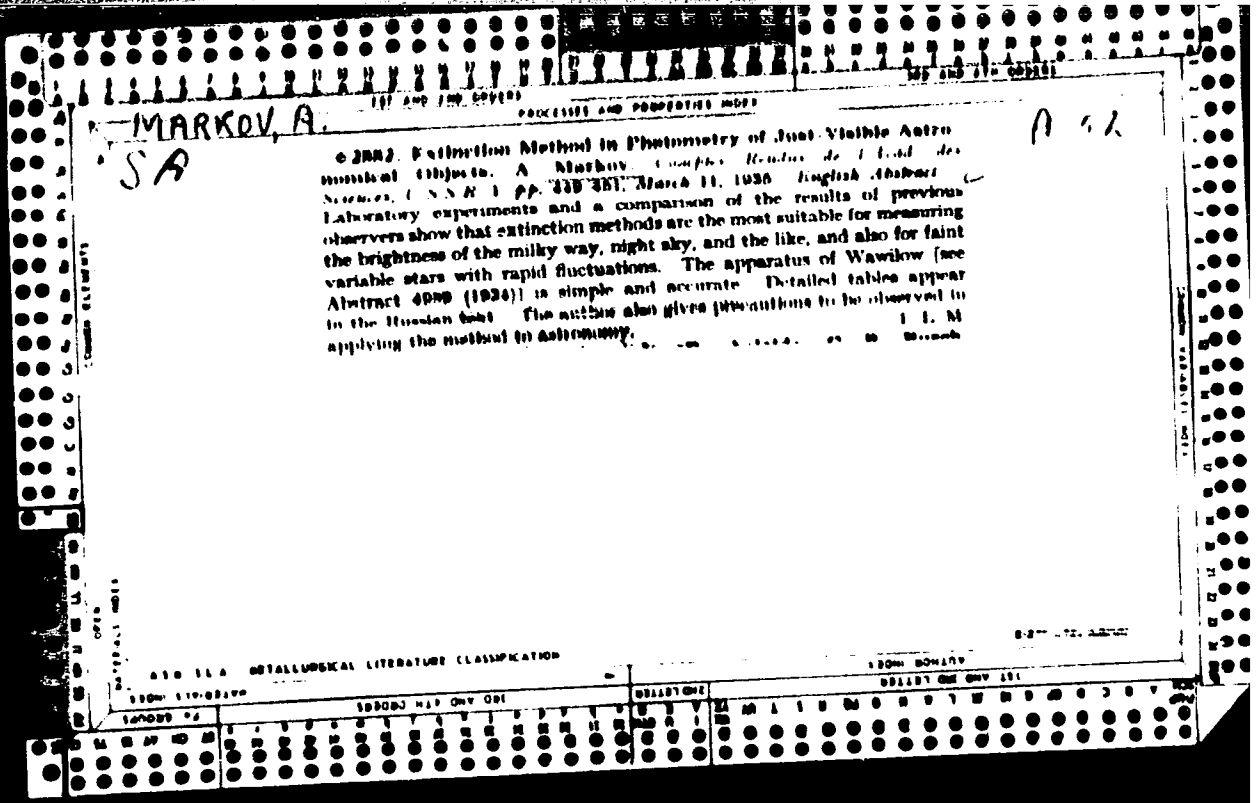
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MARKOV, A. A. (Andrey Andreyevich)

Nevozmozhnost' nekotorykh algoritmov v teorii assotsiativnykh sistem. DAN, 55 (1947), 587-590. Nevozmozhnost' nekotorykh algoritmov v teorii assotsiativnykh sistem., II DAN, 58 (1947), 353-356. O predstavlenii rekursivnykh formul. DAN, 58 (1947), 1891-1892. On the representation of relatively definite functions. Matem. SB. 4(46), (1938). On the determination of the number of roots of an algebraic equation situated in a given domain. Matem. SB., 7(49), (1946), 3-6. O svobodnykh topologicheskikh grupakh. DAN, 31(1941), 290-302.

SO: Mathematics in the USSR., 1917-1947  
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Moscow-Leningrad, 1948

MARKOV, A.A. Continued

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- O sushchestvovanii integral'nogo invarianta. Dan, 17 (1937), 455-458.
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MARKOV, A. A.

Mbr., Mathematics Inst. im. V. A. Steklov, Dept. Physico-Math. Sci., A.S.

"On Unconditionally Closed Sets," Dok. AN, 44, No. 5, 1944

"The Impossibility of Some Algorithms in the Theory of Associative Systems" *ibid.*,  
Dok. AN, 55, No. 7, 1947

"Representation of Recursive Functions," Iz. Ak. Nauk SSSR, Ser. Matemat, 13, No. 5,  
1949

MAROV, A.A.

[Principles of the algebraic theory of braids] Osnovy algebraicheskoj teorii kos. Akademiia nauk SSSR, Moscow-Leningrad, 1945. 53 p.  
(Geometry, Differential--Projective) (MLRA 7:8)

MARKOV, A. A.

7000

Markoff, A. A. Variation principles in the theory of plasticity. Appl. Math. Mech. [Akad. Nauk SSSR. Prikl. Mat. Mech.] 11, 339-350 (1947). (Russian. English summary)

The author proves three minimum principles concerning the velocity field in an incompressible perfectly plastic solid which obeys the stress-strain relation of von Mises. The simplest of these principles is concerned with the case where the velocities are prescribed on the surface subject, of course, to the condition that the surface integral of the normal velocity component vanishes. If the velocity strain is denoted by  $\epsilon_{ij}$ , and if  $E = (\epsilon_{ij} \rho_{ij})^{1/2}$ , the minimum principle in question can be formulated as follows: among all velocity distributions which satisfy the boundary conditions and the equation of incompressibility, the actual distribution furnishes the smallest value for the volume integral of the invariant  $E$ . The author's other minimum principles are concerned with the cases where (a) the stresses are given on the surface or (b) the tangential stresses and the normal velocity. The minimum principles are used to establish uniqueness of the stresses in the interior (to within an arbitrary constant hydrostatic pressure). [The author assumes tacitly that the boundary conditions assure plastic behavior throughout the body. In many practically important cases (e.g., indentation problems) this assumption is not justified.]  
W. Prager (Providence, R. I.)

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Source: Mathematical Reviews, 1948, Vol 9, No. 2

MARKOV, A.

Markoff, A. On the impossibility of certain algorithms in the theory of associative systems. C. R. (Doklady) Acad. Sci. URSS (N.S.) 55, 583-586 (1947).

Two theorems on recursive unsolvability in associative systems with a finite set of generators and relations are stated, and proved in outline. Theorem 1 asserts the unsolvability of the word (identity) problem and is identical with a theorem of E. L. Post [see the preceding review]. The method of proof is essentially similar, making use of an earlier result of Post [Amer. J. Math. 65, 197-215 (1943); these Rev. 4, 209] and Rosser's combinatorial logic [Ann. of Math. (2) 36, 127-150 (1935)]. Theorem 2 states that an associative system can be constructed in which the word problem is solvable but the division problem is unsolvable, i.e., the question whether  $XQ \leftrightarrow R$  has a solution in the system for any given  $Q$  and  $R$ . Let  $A$  be a finite alphabet and  $G_i, G'_i$  ( $i=1, 2, \dots, m$ ) words in it such that the word problem is unsolvable under the one-way substitution laws " $G_i P \rightarrow P G'_i$ " for any word  $P$ " [Post, op. cit. (1943)]. Then a system for theorem 2 is obtained by adding the new letters  $d_i, f_i, e_i$  to the alphabet and taking as relations  $e_i f_i \leftrightarrow f_i e_i, e_i G_i a \leftrightarrow a e_i G'_i, e_i G_i d_i \leftrightarrow G'_i d_i$  ( $a \in A, i=1, \dots, m$ ).

M. H. A. Newman (Manchester).

Source: Mathematical Reviews,

Vol. 8 No. 10.

MARKOV - A

2

Markov, A. On certain insoluble problems concerning matrices. Doklady Akad. Nauk SSSR (N.S.) 57, 539-542 (1947). (Russian)

Let a square matrix with integers as elements and determinant 1 be called "admissible." If  $\{X_1, X_2, \dots, X_p\}$  a finite set of admissible  $n$ -matrices, the semi-group of all matrices expressible as products of  $X_i$ 's is denoted by  $S(X_1, X_2, \dots, X_p)$ . Theorem 1. If  $n \geq 4$  there is no algorithm (in the sense of Church-Kleene-Turing) for deciding whether, given two finite sets,  $X_1, X_2, \dots, X_p$  and  $Y_1, Y_2, \dots, Y_q$  of admissible  $n$ -matrices, the sets  $S(X_1, X_2, \dots, X_p)$  and  $S(Y_1, Y_2, \dots, Y_q)$  have a common member. Moreover (corollary) all the  $Y$ 's, and all  $X$ 's but one, can be chosen and fixed, so that the question remains undecidable when the remaining  $X$  varies; the number  $q$  can here be 2, and  $p$  can also be chosen independent of  $n$ .

Proof. By a theorem of E. L. Post [Bull. Amer. Math. Soc. 52, 264-268 (1946); these Rev. 7, 405] there is no algorithm for deciding whether, given  $p$  pairs,  $G_i, G_i'$  of words in two letters,  $a$  and  $b$ , there exists an identity  $G_1 G_2 \dots G_p = G_1' G_2' \dots G_p'$ ; and Post's proof shows that all the  $G$ 's and all but one of the  $G$ 's can be chosen so that the question is still undecidable when the remaining  $G$  varies. The two matrices

$$A = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}, \quad B = \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}$$

generate a free semi-group  $S(A, B)$  [J. Nielsen, Danske Vid. Selsk. Math.-Fys. Medd. 5, no. 12 (1924)]. Hence the question whether, given  $p$  pairs of matrices  $Z_i, Z_i'$ , each equal to  $A$  or  $B$ , there exists a relation  $\prod Z_i = \prod Z_i'$ , is undecidable; or, what is the same, the question whether some  $\prod (Z_i + Z_i')$  is in  $S(A+A, B+B)$ , where  $+$  denotes the direct sum ( $4$ -matrix). This proves the case  $n=4$ , and the extension to  $n>4$  is trivial.

Theorem 2. If  $n \geq 4$  there is no algorithm for deciding whether, given admissible  $n$ -matrices  $X_1, X_2, \dots, X_p$  and  $Y_1, Y_2, \dots, Y_q$ , the set  $S(X_1, X_2, \dots, X_p)$  and the additive group  $L(Y_1, Y_2, \dots, Y_q)$  generated by the  $Y$ 's, have a common member. All the  $Y$ 's, and all the  $X$ 's but one, can be fixed [corollary 1]; or all the  $X$ 's can be fixed [corollary 2]; and the question is still undecidable when the remaining  $X$ , or the  $Y$ 's, vary. (Here  $q$  can be 5, and  $p$  independent of  $n$ .) This is proved similarly, by taking  $Y_1, Y_2, Y_3, Y_4$  to be the four  $4$ -matrices  $F_{rs} = E_{rs} + E_{rr}$ , where  $E_{rs}$  has 1 in position  $(r, s)$  and 0 elsewhere. Then  $L(Y_1, Y_2, Y_3, Y_4)$  consists of all matrices  $Z+Z$  ( $Z$  admissible).

M. H. A. Newman (Manchester).

Source: Mathematical Reviews,

1948, Vol 9, No. 5

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MARKOV, A.

Markov, A. The impossibility of certain algorithms in the theory of associative systems. II. Doklady Akad. Nauk SSSR (N.S.) 58, 353-356 (1947). (Russian)

The first part of the paper is concerned with sharpening the author's theorems 1 and 2 [same Doklady (N.S.) 55, 583-586 (1947); these Rev. 8, 558] on the unsolvability of the word problem in associative systems [demi-groups, Thue systems], and on the unsolvability of the division problem ("has  $XQ \leftrightarrow R$  a solution for given  $Q$  and  $R$ ?"), respectively. (Notations:  $X \vdash Y$  means that word  $X$  may be replaced by word  $Y$ ,  $X \perp Y$  means  $X \vdash Y$  and  $Y \vdash X$ ,  $X \leftrightarrow Y$  means that  $PXQ \perp PYQ$  for any  $P$  and  $Q$ .) (A) A system may have a solvable word problem and solvable left-division problem, but unsolvable right-division problem,  $XH_1 \leftrightarrow R$ ; and here

Source: Mathematical Reviews, Vol 9 No. 7

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*Markov, A.*

$H_1$  can be a fixed word. (B) An associative system is given having no decision algorithm for  $X \leftrightarrow 0$  (the empty word). Proofs rest on E. L. Post's unsolvable word problem under a set of one-way substitutions  $G_i P \vdash PG_i'$  ( $i = 1, 2, \dots, m$ ),  $G_i$  and  $G_i'$  fixed,  $P$  arbitrary [Amer. J. Math. 65, 197-215 (1943); these Rev. 4, 209].

In the second part of the paper a new step is taken by the construction of a class of associative systems with unsolvable word problem, having only a moderate number of defining relations which can easily be written out without abbreviation. In examples hitherto constructed the relations contain in effect a specification of the class of recursive functions and are correspondingly complicated. From the sparse indications given in the present paper, it appears that the complications are transferred from the relations to the class of words within the system for which the equivalence problem is posed. The main theorem is as follows. The alphabet consists of  $(a, b, c, d, e)$ . Let  $V$  be an arbitrary word in the letters  $a$  and  $b$ , and  $U$  any word in  $a, b, c, d$  beginning and ending with  $d$ , in which every two  $c$ 's are separated by at least one  $d$ . Then there is no algorithm for deciding whether  $UeV$  goes into  $Uea$  by means of the single rule (a)  $PdQzRdSeQT \vdash PdQzRdSdTR$ , where  $P, S, T$  are arbitrary words in  $a, b, c, d, e$ ;  $Q$  and  $R$  arbitrary words in  $a, b$ . The following two results are to be used in the proof. (1) In the problem of Post referred to above the one-way substitutions  $G_i P \vdash PG_i'$  may be replaced by symmetrical ones  $K_i P \vdash PK_i'$ . [Cf. lemma II of Post, J. Symbolic Logic 12, 1-11 (1947); these Rev. 8, 558.] (2) If  $L_i, L_i'$  ( $i = 1, \dots, q$ ),  $V, W$  are words in  $a, b$ , a necessary and sufficient condition that  $V$  go into  $W$  by means of  $L_i P \vdash PL_i'$  is that  $dL_i cL_i' \dots dL_i cL_i' deV$  goes into  $dL_i cL_i' \dots dL_i cL_i' deW$  by means of (a). An associative system  $C_3$  on 13 letters is given, with 33 defining relations  $X \leftrightarrow Y$ , where no  $X$  or  $Y$  contains more than three letters, which can be shown by the main theorem (presumably using the examples constructed in the first part of the paper) to have an undecidable word problem; in a slightly more complicated system  $C_4$  the problem  $X \leftrightarrow H_3$  is undecidable, where  $H_3$  is a fixed 3-letter word. No details of the proof are given.

*M. H. A. Newman (Manchester).*

Source: Mathematical Reviews *AM* *2/2* Vol *7* No. *7*

MARKOV, A. [A.]

Markov, A. On the representation of recursive functions.  
Doklady Akad. Nauk SSSR (N.S.) 58, 1891-1892 (1947).  
(Russian)

S. C. Kleene has proved (A) that every general recursive function of  $n$  variables can be represented in the form

$$(1) \quad P(\mu y \cdot Q(x_1, \dots, x_n, y) = 0),$$

where  $P$  and  $Q$  are primitive recursive, and  $\mu y \cdot X$  is the least natural number  $y$  such that  $X$  holds, or 0 if there is none [Math. Ann. 112, 727-742 (1936)]; and (B) that a fixed "universal" primitive recursive function  $P$  can be found, such that all general recursive functions are obtained by suitable choice of primitive recursive  $Q$  in (1) [Trans. Amer. Math. Soc. 53, 41-73 (1943); these Rev. 4, 126]. In the present note the theorem is announced [without proof] that a necessary and sufficient condition for a primitive recursive function  $P(x)$  to be universal, in the above sense, is that it takes every natural number as value an infinity of times.

M. H. A. Newman (Manchester).

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Source: Mathematical Reviews

Vol 9 No 8

*M.A.R.K.O.V. A. A.*

*2/20*

\* Markov, A. A. Izbrannye Trudy po Teorii Nepreryvnykh  
Dobrykh Funktsii Naimen'ee Uklonyayushchisya ot  
Nulya. [Selected Papers on Continued Fractions and  
the Theory of Functions Deviating Least from Zero].  
OGIZ, Moscow-Leningrad, 1948. 411 pp.  
Contains a biography and notes by N. I. Ahiezer.

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Source: Mathematical Reviews,

Vol 11 No. 3

MARKOV, A. A.

Markov, A. A. On the dependence of axiom B6 on the  
~~other axioms of the Bernays-Gödel system.~~ Izvestiya  
Akad. Nauk SSSR. Ser. Mat. 12, 569-570 (1948).  
(Russian)

Simplification of the system of axioms for set-theory  
given by Bernays [J. Symbolic Logic 2, 65-77 (1937)] and  
modified by Gödel [The Consistency of the Continuum  
Hypothesis, Princeton University Press, Princeton, N. J.,  
1940; these Rev. 2, 66]. A. Heyting (Amsterdam).

*Handwritten initials*

Source: Mathematical Reviews.

Vol 10 No. 7

МАРКОВ, А. А.

Markov, A. A. On the representation of recursive functions. Izvestiya Akad. Nauk SSSR. Ser. Mat. 13, 417-424 (1949). (Russian)

This paper gives a detailed proof that a necessary and sufficient condition that a primitive recursive function  $P(x)$  be such that every recursive function of  $n$  variables can be represented, for suitable primitive recursive  $Q$ , in the form  $F[\lambda y. Q(x_1, \dots, x_n, y) = 0]$  is that  $P(x)$  take every natural

number as value infinitely many times. This result was announced earlier [Doklady Akad. Nauk SSSR (N.S.) 58, 1891-1892 (1947); these Rev. 9, 403]. The sufficiency part is constructive in terms of certain results of Kleene's [cited in the above-mentioned review]; the necessity proof is non-constructive, but has a weakened constructive counterpart.

H. B. Curry (State College, Pa.)

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Source: Mathematical Reviews,

Vol. 11 No. 3

MARKOV, A. A.

Markov, A. A. Three papers on topological groups: I. On the existence of periodic connected topological groups. II. On free topological groups. III. On unconditionally closed sets. Amer. Math. Soc. Translation no. 30, 120 pp. (1950).  
Translated from Izvestiya Akad. Nauk SSSR. Ser. Mat. 8, 225-232 (1944); 9, 3-64 (1945); Mat. Sbornik (N.S.) 18(60), 3-28 (1946); these Rev. 7, 7, 412.

Source: Mathematical Reviews.

Vol 12 No. 5

MARKOV, A. A.

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USSR/Mathematics - Approximations

Jul/Aug 51

"Ideas of P. L. Chebyshev and A. A. Markov in the Theory of Limit Magnitudes of Integrals and Their Further Development," M. G. Kreyn, P. G. Rekhtman

"Uspekhi Matemat Nauk" Vol VI, No 4 (44), pp 3-120

Discusses fundamental theorem concerning positive sequences, max mass, main properties of Chebyshev's system of functions, canonical representations of a positive sequence, existence of the main representations, motion of the masses of canonical representations, mech quadratures and soln of an extremal problem, Chebyshev-Markov inequalities, case of infinite integral, the phi-psi problem of Markov, and a min problem.

191T75



MARKOV, A. A.

Markov, A. A. The theory of algorithms. Trudy Mat. Inst. Steklov., v. 38, pp. 176-189. Izdat. Akad. Nauk SSSR, Moscow, 1951. (Russian) 20 rubles.

The author considers that the Church-Kleene-Turing theory of computability touches the idea of "algorithm" so indirectly as to make an independent development desirable. After somewhat lengthy preliminaries (e.g. definition of an "occurrence" of one word in another) an "algorithm  $\mathcal{A}$  in normal form" is defined as follows. It is (or is determined by) a list of instructions in one of the forms

$$P \rightarrow Q \text{ or } P \rightarrow \cdot Q,$$

where  $P$  and  $Q$  are words in some alphabet; either or both of  $P$  or  $Q$  may be the empty word (i.e. absent). Thus  $ab \rightarrow ba$  and  $a \rightarrow \cdot$  and  $\rightarrow$  are possible instructions. The order of the instructions in the list must be specified. To apply the algorithm to a given word  $X$ , take the first instruction in the list whose left-hand side occurs in  $X$  (the empty word occurs before and after every letter), and replace the first occurrence of  $P$  by  $Q$ . If there is a dot after the arrow this ends the process; if not, apply  $\mathcal{A}$  in the same way to the resulting word; and so on. If the process terminates the final result is  $\mathcal{A}(X)$ .

In support of the claim that this gives a satisfactory meaning of "algorithm" it is asserted that (1) every algorithm  $\mathcal{A}$  in the rather vague sense of ordinary mathematics, is equivalent to some normal algorithm  $\mathcal{N}$ , i.e. applied to any given word  $X$ ,  $\mathcal{N}$  terminates if and only if  $\mathcal{A}$  does, and then  $\mathcal{N}(X) = \mathcal{A}(X)$ ; (2) various specified combinations of normal algorithms (iteration, juxtaposition of results, etc.) are equivalent to normal algorithms; (3) a "universal normal algorithm"  $\mathcal{U}$  exists such that, if the instructions specifying  $\mathcal{A}$  are combined in an obvious way (with spacing symbols) into a single word  $\mathcal{A}^*$ ,  $\mathcal{U}(\mathcal{A}^*P) = \mathcal{A}(P)$  (if either exists,  $\mathcal{A}^*P$  denoting mere juxtaposition). No indications of the proofs are given. The word  $\mathcal{A}^*$ , translated into a 2-letter alphabet, is the "signature" of the algorithm  $\mathcal{A}$ . A normal algorithm is "self-applicable" if its application to its own signature terminates. There is no normal algorithm which terminates for just those words that are signatures of non-self-applicable

Source: Mathematical Reviews,

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normal algorithms (proved by the usual Cantor-type argument). It follows by familiar arguments that the range of  $\mathcal{U}$  (above) is not discernible, i.e. there is no normal algorithm  $\mathcal{A}$  that terminates for every  $X$  and is such that  $\mathcal{A}(X)$  is the empty word if and only if  $\mathcal{U}$  terminates when applied to  $X$ .

In spite of his initial references, the author makes no mention of the question that will occur to every reader: what is relation between "normal algorithms" and computability à la Church-Kleene-Turing? It is obvious that normal algorithms can be programmed on a computing machine, indeed they resemble instruction-tables for existing machines a good deal more closely than do the tables for Turing's original "paper" machine [Proc. London Math. Soc. (2) 42, 230-265 (1936)]. The strong resemblance between the general course of this theory and Turing's [op. cit.] makes it likely that there is full equivalence. If that is so the interest of this theory will lie in its provision of a new and particularly simple means of constructing unsolvable problems. [In the "theorem on a universal algorithm", foot of p. 184, for the first two occurrences of  $\mathcal{A}$  read  $\mathcal{U}$ .]

M. H. A. Newman (Manchester).

Source: Mathematical Reviews,

Vol. 13 No. 9

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MARKOV, A.

Source: Markov, A. The impossibility of certain algorithms in the theory of associative systems. Doklady Akad. Nauk SSSR (N.S.) 77, 19-20 (1951). (Russian)

In this review (but not in the paper)  $[C, A]$  or  $[C]$  denotes the associative system determined in the alphabet  $A$  by the set of relations  $C$ . The problem of the existence of algorithms for deciding the following questions is considered: given an alphabet  $A$  and finite sets  $C_1$  and  $C_2$  of relations, (1) are  $[C_1]$  and  $[C_2]$  isomorphic? (2) does  $[C_1]$  contain only one member? (3) is it a group? (4) contained in a group? (5) is it a semi-group [with cancellation]? (6) ("the meta-problem of identity") is  $[C_1]$  a system in which the identity-problem [= word-problem] is solvable? A negative answer is given in all six cases: no such algorithms exist for an alphabet with 4 or more letters.

An outline of the proof is given. A system  $[C, A_1]$  of an earlier paper [same Doklady (N.S.) 58, 353-356 (1947); these Rev. 9, 321] is first transformed by Post's method [E. L. Post, Bull. Amer. Math. Soc. 50, 284-316 (1944); these Rev. 6, 29] into a system  $[D, A_0]$  where  $A_0$  is the 2-letter alphabet  $\{a, b\}$ . Given any two words  $G, H$  of  $A_0$ , let  $D_{a, \pi}$  be the set of relations in  $B = \{a, b, c, d\}$  formed by adjoining the relations  $cGd \leftrightarrow 0$  and  $\{cHd \leftrightarrow cHd\}$  ( $\{ = a, b, c, d$ ) to  $D$ . In the system  $[D_{a, \pi}, B]$  the answer to questions (2) to (6) is "Yes" if, and only if,  $G \leftrightarrow H$  in  $[D, A_0]$ . Since  $[C, A_1]$ , and therefore also  $[D, A_0]$ , has an unsolvable word problem [Markov, as above] this proves the unsolvability of (2) to (6), and that of (1) follows.

M. H. A. Newman (Manchester).

*John*

MARKOV, A.

Markov, A. The impossibility of algorithms for the recognition of certain properties of associative systems. Doklady Akad. Nauk SSSR (N.S.) 77, 953-956 (1951). (Russian)

A general theorem is announced, with an outline proof, from which the results of a previous paper [same vol., 19-20 (1951); these Rev. 12, 661; called M1 in this review] follow as special cases. Let "K-system" mean "associative system with a finite set of generating relations". A K-system,  $S$ , is said to be included in another,  $T$ , if  $S$  is isomorphic to a subsystem of  $T$ . A property  $P$  of K-systems is invariant if it is preserved under isomorphisms. As in the cited review, we denote by  $[R, A]$  the K-system defined by the relations  $R$  in the alphabet  $A$ . The "recognition problem" for a property  $P$  and an alphabet  $A$  is the problem of finding an algorithm for deciding, for any finite set of relations  $R$  in  $A$ , whether or not  $[R, A]$  has the property  $P$ . Theorem 1. Let  $P$  be an invariant property of K-systems. If there exist both a K-system having the property, and a K-system not included in any K-system having the property, then there exists an alphabet for which the recognition problem for  $P$  is unsolvable. If a K-system with the property  $P$  is definable with  $n$  letters, the recognition problem for  $P$  is unsolvable for alphabets of  $\geq n+4$  letters.

The method of proof is a generalisation of that used in M1, the relations  $D$  and alphabet  $B = \{a, b, c, d\}$  of that paper being replaced by  $R_1 \cup R_2$  and  $B \cup B_1$ , respectively, where  $R_1, R_2$  and  $B_1$  are as follows.  $[R_1, \{a, b\}]$  is a K-system that includes (in the above sense) the "direct product" of a

K-system  $S_1$  having an unsolvable word-problem, and a K-system  $S_0$  not included in any having property  $P$ . (Here the "direct product" of  $[R, A]$  and  $[R', A']$  is  $[R \cup R', A \cup A']$ , provided that  $A \cap A' = \emptyset$ .) The system  $[R_1, B_1]$  is a K-system having property  $P$ , such that  $B \cap B_1 = \emptyset$ . An immediate corollary of the theorem is that if  $P$  is a hereditary property, i.e., holds for all subsystems of K-systems that have the property, and if there exist K-systems that have, and K-systems that have not the property, then the recognition problem is unsolvable for alphabets of 4 or more letters. A deduction from the main theorem not included in M1 is that there is no algorithm for deciding if a given K-system is finite.

M. H. A. Newman (Manchester).

Source: Mathematical Reviews,

Vol. 5 No.

Markov, A

Markov, A. On an unsolvable problem concerning matrices. Doklady Akad. Nauk SSSR (N.S.) 78, 1089-1092 (1951). (Russian)

The following theorem is proved. If  $n \geq 6$ , a set of  $102$   $n$ -rowed square matrices  $U_i$  with rational integral elements can be found, such that the problem of deciding whether any given integral matrix  $U$  of the same size is expressible as a finite product  $\prod U_i$  is unsolvable (in the usual sense, that no algorithm or machine routine exists). The proof, which is given in full, depends on an earlier unsolvability theorem of the author on matrices [same Doklady 57, 539-542 (1947); these Rev. 9, 221]. The transformation of the one problem into the other depends on ingenious but elementary algebra. The author believes that the number  $102$  can probably be lowered. M. H. A. Newman (Manchester).

*SMW*

Source: Mathematical Reviews,

Vol 13

No 2

MARKOV, A. A.

"Impossibility of Certain Algorithms in the Theory of Associative Systems,

Dok. AN, Vol. 78, No. 1, 1951

Discusses following problems which arise in study of associative systems defined by finite systems of relations in given algebra A: isomorphy, unity, uniqueness, recognition of groups, inclusiveness in group, recognition of subgroup, and meta-problem of identity. Finds for each letter A containing more than 2 letters each of the above problems is unsolvable: The sought-for algorithm in this problem is impossible. Submitted 4 Jan 51 by Acad I. M. Vinogradov

170P47

DELONE, B.N.; KURCSH, A. G.; KOLMOGOROV, A. N.; MARKOV, A. A.; GELFOND, A. G.;

Algebra

Development of algebra. Usp. mat. nauk 7 No. 2, 1952.

9. Monthly List of Russian Accessions, Library of Congress, November <sup>2</sup> 195~~3~~, Incl.

Jul/Aug 52

USSR/Mathematics - Symbolic Logic  
Unsolvability  
A.A. Markov,

"Unsolvable Algorithmic Problems," No 1, pp 34-42  
Leningrad

"Matemat Stor" Vol XXXI (73), No 1, pp 34-42

A lecture given at conference on algebra and  
number theory in Moscow in Sep 51, representing  
a summary of results obtained by the author in  
recent years in the theory of algorithms. By  
"algorithm" one understands an exact instructional  
(order or direction) which defines a computational  
220713

process proceeding from original data that can be  
varied to the desired result. Cites E.L. Post,  
"Recursive Unsolvability of a Problem of Thue,"  
Jour of Symbolic Logic, 12, 1947, 1-11.  
Submitted 22 Feb 52.

MARKOV, A. A.

220713



200T75

MARKOV, A. A.

USSR/Mathematics - Algorithm Theory 21 May 53

"Strengthening the Theorem of Reduction (Adduction) in the Theory of Algorithms," N. M. Nagornyy

DAN SSSR, Vol 90, No 3, pp 341-342

Strengthens the theorem given by A. A. Markov (Trudy Matemat In-ta imeni Steklova, 38 (1951)) as a consequence of the theorem on algorithm reduction. This theorem states that each normal algorithm over alphabet A is equivalent relative to A to a certain normal algorithm in the alphabet  $A \cup \{a, b\}$ , where a and b are letters not belonging in A. The

260T75

theorem permits one to reduce any normal algorithm over alphabet A to an equivalent, relative to A, normal algorithm in a 2-letter expansion of alphabet A. Acknowledges attention of Prof A. A. Markov. Presented by Acad V. I. Smirnov 18 Mar 53.

MARKOV, A. A.

USSR/Mathematics - inequalities 11 0 0 0 0

"Generalization of Inequalities of S. N. Bernshtey and A. A. Markov," N. K. Bari

DAN SSSR, Vol 90, No 5, pp 701-702 (1963)

Subject inequalities and those of A. Zygmund are widely used in studying the best approximations of a function by means of trigonometric polynomials and also in investigating convergence and summability of Fourier series and their conjugates; however, in order to utilize these inequalities one must know what properties are possessed by the considered function on an interval of length  $2\pi$ , which means that, if the

260T76

function's behavior is investigated on an interval  $[a, b]$  of length less than  $2\pi$ , the corresponding theorems lose some force. Generalize 3 theorems apropos of this case. Presented by Acad A. N. Kolmogorov.

MARKOV, A.A.; PETROVSKIY, I.G., akademik, redaktor; NIKOL'SKIY, S.M., professor; SAZONOV, L.S., redaktor; AROKS, R.A., tekhnicheskiy redaktor.

Theory of algorithms. Trudy Mat.inst. 42:3-374 '54. (MIRA 8:5)  
(Algorism)

MARKOV, A. A.

"Work of Soviet Mathematicians in the Domain of Constructive Analysis,

"On the Principle of Constructive Selection,"

paper either presented or distributed at the Intl. Colloquium on the Different  
Notions of Constructivity in Mathematics, 26-31 Aug 57, Amsterdam,

B-3,095,946, 20 Jan 1958

**AUTHOR:** Markov, A.A., Corresponding Member of the AN USSR 30-8-3/37

**TITLE:** Mathematical Logic and Determination Mathematics (Matematicheskaya logika i vychislitel'naya matematika)

**PERIODICAL:** Vestnik Akademii Nauk SSSR, 1957, Vol.27, Nr 8, pp.21-25 (USSR)

**ABSTRACT:** The author at first gives explanatory specifications on the reciprocal connection between the two fields of science mentioned above. One of the basic methods of mathematical logic is the construction of proof. Formulating of the axioms and theorems is, by making use of a special system of symbolics, represented by the usual formulae. After concrete specifications on the "method of determination" the author gives an example for one of these possibilities (in form of an equation proof, see page 22). In conclusion the author deals with algorithms and underlines their great importance in mathematical logics. An important task is imposed upon mathematical logics with respect to the programmatical working through of the further development of electron computation machines. It may be expected that the attitude towards

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Mathematical Logic and Determination Mathematics

these problems will have a stimulating effect on one of the most important fields of mathematical logic, the algorithm theory.

AVAILABLE: Library of Congress

Card 2/2

*M. A. K. 1.1*

**AUTHOR:** MARHOV, A.A. Corresponding Member Acad. Sc. USSR 01-2-5, 42  
**TITLE:** On the Inversion Complexity of Function Systems (ob inverzionnoy slozhnosti sistem funktsiy)  
**PERIODICAL:** Doklady Akad.Nauk, SSSR, 1957, Vol.116, Pt 6, pp. 117-119 (USSR)  
**ABSTRACT:** Generalizing E.N. Gilbert's investigations (ref. 2) concerning the inversion complexity of a Boolean function the author considers the inversion complexity  $\text{Inv}(f_1, \dots, f_m)$  of a system  $f_1, \dots, f_m$  of  $m$  Boolean functions of  $n$  arguments.

Let the maximum  $\text{Inv}(f_1, \dots, f_m)$  of the  $2^{m2^n}$  different systems  $f_1, \dots, f_m$  be  $I(n, m)$ . Then it is: 1.  $I(n, 1) = \text{pd}(n+1)$  and 2.  $I(n, m) = D(n)$  for  $m > 1$ . Here  $D(r)$  is the smallest natural number  $y$  for which it holds  $r < 2^y$ , and  $\text{pd}(r)$  is the integer of least distance to  $r$  which is not greater than  $r$ . If particularly it is  $m = 1$ , then it is

$$\text{Inv}(f) = \text{pd}(D(\text{Alt}(f)))$$
,  
 whereby it is  $0 \leq \text{Alt}(f) \leq n+1$  and the symbol  $\text{Alt}(f)$  is defined by certain alternating chains. There are 2 references,

Card 1/2

On the Inversion Complexity of Function Systems

70-6-5, 42

1 of which is Slavic.

ASSOCIATION: Mathematics Institute imeni V. A. Steklov, Acad. Sc. USSR  
(Matematicheskiy institut im. V. A. Steklova Akademii nauk SSSR)

SUBMITTED: May, 17, 1957

AVAILABLE: Library of Congress

Card 2/2



16(1)

MARKOV, A A

SOV/1707

PHASE I BOOK EXPLOITATION

Akademiya nauk SSSR. Matematicheskii institut

Problemy konstruktivnogo napravleniya v matematike; sbornik rabot, vyp. 1 (Problems Connected With the Construction Trend in Mathematics; Collection of Articles, Nr 1) Moscow, Izd-vo AN SSSR, 1958. 348 p. (Series: Its: Trudy, t. 52). 2,500 copies printed.

Ed.: N.A. Shanin; Resp. Ed.: I.G. Petrovskiy, Academician; Deputy Resp. Ed.: S.M. Nikol'skiy, Professor; Tech. Ed.: R.A. Arons.

PURPOSE: This book is intended for mathematicians.

COVERAGE: The book is a collection of works presented at the seminar on mathematical logic of the Leningrad Branch of the Matematicheskii institut imeni V.A. Steklova (Mathematical Institute imeni V.A. Steklov) of the Academy of Sciences, USSR. The articles deal primarily with problems connected with the constructive trend in mathematics. A detailed study is made of the theory of algorithms and constructive mathematical logic. The book is divided into

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Problems Connected With the Construction (Cont.)

SOV/1707

three main parts: I. The General Theory of Algorithms and Its Application to the Theory of Associative Calculations. II. Constructive Mathematical Logic. III. Constructive Mathematical Analysis.

TABLE OF CONTENTS:

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Nagornyy, N.M. Certain Generalized Concepts of a Normal Algorithm 7

Introduction 1. Definition of  $\omega$ -type algorithms 2. Closure of  $\omega$ -type algorithms 3.  $\omega$ -type algorithms and normal algorithms 4.  $\omega$ -type algorithms and normal algorithms (continuation) 5. Canonical  $\omega$ -type algorithms 6. Composition of  $\omega$ -type algorithms 7. Branching of  $\omega$ -type algorithms 8. Recursion of  $\omega$ -type algorithms 9.  $\omega$ -type algorithms 10.  $\omega$ -type algorithms. References

Nagornyy, N.M. On the Minimum Alphabet of Algorithms Over a Given Alphabet

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Problems Connected With the Construction (Cont.)

SOV/1707

Detlovs, V.K. The Equivalence of Normal Algorithms and Recursive Functions

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Orlovskiy, E.S. Certain Problems of the Theory of Algorithms

140

Introduction I. Construction of normal algorithms inverse to a given algorithm 1. Formulation of provable theorems 2. Construction of unknown algorithms 3. Proof of theorem 2 II. Construction of a universal algorithm system 4. A universal algorithm system 5. Fundamental lemmas 6. Proof of fundamental lemmas. References

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Tseytin, G.S. Associative Calculation With the Unsolvable Problem of Equivalence	172
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1. Constructive mathematical objects 2. Historical information. Critique of S.C. Kleene's theory 3. Fundamental logicomathematical languages 4. Algorithms of the behavior of a constructive problem 5. An algorithm for deciphering elementary formulas 6. On the meaning of supporting formulas 7. Some information from the constructive theory of sets 8. Certain extensions of fundamental logicomathematical languages	

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Problems Connected With the Construction (Cont.)

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PART III. CONSTRUCTIVE MATHEMATICAL ANALYSIS

Markov, A.A. On Constructive Functions

315

Introduction 1. Recursive functions with rational values  
2. Regularly converging sequences 3. Constructive real  
numbers 4. Constructive sequences of real numbers 5. Con-  
structive functions of a real variable. References

AVAILABLE: Library of Congress

Card 5/5

LK/ad  
6-15-59

MARKOV A D

AUTHOR: None Given.

TITLE: All-Union Conference on the Theory of Relay Systems.  
(Vsesoyuznoye soveshchaniye po teorii i primeneniyu rel'nykh deystviya).

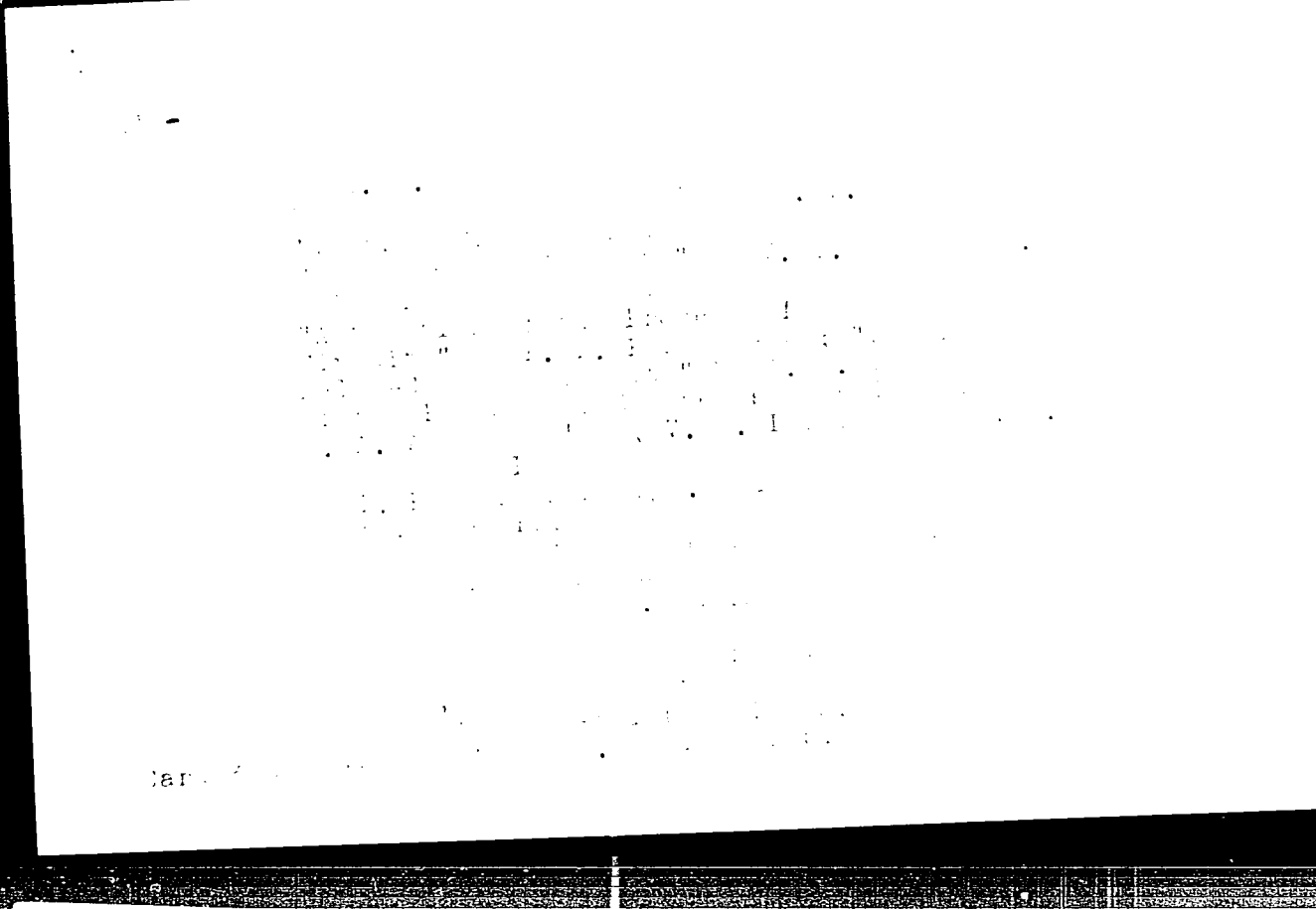
PERIODICAL: Izvestiya Akademii Nauk SSSR, Otdeleniye Inzhenernykh Nauk, 1958, No.2, pp. 167-168 (USSR).

ABSTRACT: The Institute of Automation and Telemechanics of the Ac. Sc. USSR (Institut Avtomatiki i Telemekhaniki Akademii Nauk SSSR) convened in October, 1957 an All-Union Conference on the theory of relay systems. The aim of the conference was to evaluate the present state of the problem of the theory of relay operation, particularly evaluation of the problems of synthesis, optimization, transformation of the structure of relay equipment, optimum construction and assembly of such structures, automation of the processes of synthesis and analysis of such structures. Over 240 representatives of scientific establishments, works' laboratories and design bureaus from numerous centers of the USSR and 100 scientists from Roumania, Hungary and Czechoslovakia participated in the conference.

Card 1/5 In his opening address M. A. Gavrilov reported on the

All-Union Conference on the Theory of Relay Elements, 1964 (1965)  
 present state and the main trends of development of  
 the theory of relay circuits.  
 Thirty papers were read including: "On the Theory of  
 of Mathematical Logic and Its Engineering Applications"  
 by S. A. Yanovskiy, "Algebraic Theory of Contact Circuits"  
 of Relay-Contact Circuits" by G. K. Mikhlin, "On the  
 "On the Invariant Computability of S.S. Functions"  
 by A. A. Merlov, "Minimal Disjunctive Normal Form of  
 Functions" by I. Popovic (Belgrade), "On the  
 mathematical Foundations of the Theory of Relay Circuits"  
 by S. V. Yefremov.  
 The technical applications of the theory of relay circuits  
 in the field of: "Technical Design of Digital  
 Minimal Number of Relays Necessary for the Realization  
 of a Relay Circuit with Given Conditions of Operation"  
 V. G. Izrael; "Matrix Method of Calculation of Logical  
 Functions in the Theory of Contact Circuits" by A. I. Ilyin,  
 "On the Theory of Synthesis of Contact Circuits"  
 F. Seebach (Prague); "Construction of Relays with  
 with Bridge Connection" by K. A. Gerasimov; "On the  
 Synthesis of Multi-Pole Relay-Contact Circuits"  
 V. N. Gadenchikov; "Application of the Method of

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All-Union Conference on the Problem of Reliability of structure of relay equipment. For further development, particularly for the synthesis of structures. The conference pointed out the advisability of a combined commission relative to of relay systems of establishing an International Federation relative to this problem.

(Note: Full text available in Russian.)

AVAILABLE: Library of Congress.

Card 5/5

MARKOV, A.

"Mathematical logic and computational mathematics. Tr. from the Russian"  
Fiziko-Matematicheskoe Spisanie. Sofia, Bulgaria. Vol. 1, no. 3/4, 1958

Monthly list of East European Accessions (FEAI), LC, Vol. 8, No. 6, Jun 59, Unclas

MARKOV, A.A.

Constructive functions. Trudy Mat. inst. 52:315-348 1958.

(MIRA 11:7)

(Mathematical analysis)

AUTHOR: Markov, A. (Corresponding Member of the Academy of Sciences of the USSR) SC7/20-121-2-6/5

TITLE: The Unsolubility of the Problem of Homeomorphy (Nerazreshimost problemy gomeomorfii)

PERIODICAL: Doklady Akademii nauk SSSR, 1958, Vol 121, Nr 2, pp 218-220 (USSR)

ABSTRACT: The determination of an algorithm with the aid of which it can be investigated whether two arbitrary given polyhedra (manifolds) are homeomorphic or not, is denoted by the author as the problem of homeomorphy. A natural restriction consists in the establishment of one of the compared polyhedra; then it has to be investigated whether the other polyhedra are homeomorphic to the given one.

Principal theorem: Let  $n > 3$ . The manifold is understood in the sense of Poincaré [Ref 4] and Veblen [Ref 5]. For every  $n$  there exists an  $n$ -dimensional manifold  $M^n$  such that the problem of homeomorphy of the manifolds to  $M^n$  is unsolvable.

In an analogous manner the problem of the homotopic equivalence is given; in this case the correspondingly changed above principal theorem is valid too.

There are 5 references, 2 of which are Soviet, 2 American, and 1 Italian.

Card 1/2

The Unsolvability of the Problem of Homeomorphy

SOV/20-121-2-6/53

SUBMITTED: March 21, 1958

Card 2/2

16(1)

AUTHOR: Markov, A. (Corresponding Member of the AS USSR) SOV/20-123-6-6/50  
TITLE: On the Unsolvability of Some Topological Problems (O nerazreshimost  
nekotorykh problem topologii)

PERIODICAL: Doklady Akademii nauk SSSR, 1958, Vol 123, Nr 6, pp 978-980 (USSR)

ABSTRACT: The present paper improves and precisises the earlier results of the author [Ref 3].

Let the complex  $K$  be related to the complex  $L$  if:  $K$  and  $L$  are connected and their fundamental groups are isomorphic, or if at least one of these complexes is not connected.

Let  $\mathcal{R}$  and  $\mathcal{T}$  be binary relations between complexes.  $\mathcal{R}$  is called stronger than  $\mathcal{T}$ , if  $K$  always has a relation  $\mathcal{T}$  to  $L$ , if  $K$  has a relation  $\mathcal{R}$  to  $L$ . Let the binary relation  $\mathcal{Q}$  lie between  $\mathcal{R}$  and  $\mathcal{T}$  if  $\mathcal{R}$  is stronger than  $\mathcal{Q}$  and  $\mathcal{Q}$  is stronger than  $\mathcal{T}$ .

Principal results: To every natural  $n > 3$  there exists a connected closed  $n$ -dimensional manifold  $M^n$  so that for every binary relation  $\mathcal{R}$  lying between the combinatoric equivalence and the relationship

the problem of distinction of the relation  $\mathcal{R}$  to  $M^n$  among the  $n$ -dimensional manifolds is unsolvable.

Herefrom there follows that the general problem of distinction of

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On the Unsolvability of Some Topological Problems

SOV/20-123-6-6.50

the combinatoric equivalence is unsolvable.

There are 5 references, 2 of which are Soviet, 2 American, and 1 Dutch.

ASSOCIATION: Matematicheskii institut imeni V.A.Steklova Akad.n.SSSR  
(Mathematical Institute imeni V.A.Steklov of the AS USSR)

SUBMITTED: October 21, 1958

Card 2/2



16.4000 (163,1344,1132)

26083

P/021/61/000,002,001,001  
A107/A126

AUTHOR: Markov, A.A., Professor, Doctor, Chairman, Corresponding Member

TITLE: Development of cybernetics in the Soviet Union

PERIODICAL: Przegląd Elektrotechniczny, no. 2, 1961, 53 - 55

TEXT: The basic element of cybernetics is the information based on associations given by the nature's order, evoking the situation A as a consequence of the previous situation B. The Soviet Mathematician A.N. Tikhonov proved that the division of the temperature of an earth stratum depends on its depth and contains information on temperature changes of the earth surface in the past. This example demonstrates the process of information arising when the temperature of the earth surface is expressed as the situation A and the temperature in the past computed according to established rules, as the situation B. If the situations A and B are divided by time or space the forwarding of information takes place. The author describes the Shannon theory and the established coding of information. Soviet scientist A.N. Kolmogorov, A.Ya. Khinchin, A.M. Yaglom and I.M. Gelfand investigated this problem, whereas A.Ya. Khinchin and V.R. Varshamov investigated the problem of coding. The synthesis of steering systems, based on contact ele-

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A107/A126

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Development of cybernetics in the Soviet Union

ments, was successfully investigated by Soviet scientists. A partial answer to the problem of the Bool function in relation to n arguments was given by Shannon. The Soviet mathematician, O.B. Lupanov, found this solution by changing n + 2 into n. This achievement is based on a new interpretation of the Bool's function and on new methods of contact synthesis expressed by

$$\frac{2^n}{n} (1 - \epsilon) < L(n) < \frac{2^n}{n} (1 + \epsilon),$$

at which the condition is a sufficient high n value. Lupanov obtained results for various additional systems based on functional elements, especially for programming computers. An example of a functional element is the alternator in which electronic valves and semi-conducting diodes are used. Similar is the system of two entries, called conjunctor. The negator is a function element registering negations. By assembling conjunctors, alternators and negators it is possible to build up unlimited Bool functions or systems related to those functions. Our nervous system can be regarded as a system of neurone functions. Evaluating the composition of such systems it is advisable to replace the number of function elements by a "weight" for each element, expressed by plus values. According to Lupanov it is possible to relate free established weights to given function elements. Analogue to the Shannon system, tolerable figures of matching weight can be used for contact systems. The author describes results of invest!

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P/021/61/000/002/001/001  
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Development of cybernetics in the Soviet Union

gations performed by the Soviet biologist Vayncvayg (Weinzweig) in the field of power engineering systems composed of functional elements. Vayncvayg assumed that energy is delivered only in case of an exit signal of an element; in this case an energy evaluation of a system is performed. The function  $\epsilon$  in case of unlimited increase of the argument was different from Shannon's function. He demonstrated that for some systems of functional elements the expression  $\epsilon(n) < Cn$  is valid, where  $C$  is a constant plus value. This assumption enables the realization of Bool function of a high number of arguments of rather complicated systems. It is probable that such a process takes place in the human brain. The author describes the practical use of cybernetics in investigation of the structure of languages and creation of artificial languages, i.e., conventional logical mathematical languages, chemical-formula languages, etc. Recently, an international algorithimical language, called "algol", for formulation of problems for computers was introduced. A.A. Iupanov worked out an operational language for programming of such problems. The mathematical linguistic which is a part of cybernetics was recently investigated by the Soviet scientists Kulagin and Dobrushin. Investigations on mechanical translations were performed in the USSR by Kulagin and Moloshny. Automatic programming based on Soviet results was developed by L.B. Kantorovich, A.P. Jershov and others. The Soviet scientist Mielchuk

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Development of cybernetics in the Soviet Union

P/021/61/000/002/001/001  
A107/A126

developed methods for translation of various languages into Russian. A team of scientists in Leningrad works on algorithms for translation into Indonesian, Burman, Vietnam and Suahely languages and vice versa. For this purpose an intermediate language was worked out. Similar investigations were performed in Kiyev, Tbilisi and Yerevan. The Soviet scientist L.V. Kantorovich works since 1930 on the development of mathematical methods for the solution of economical problems based on cybernetics. Based on this method, Leontiyev developed in the USA a method of linear programming for planning in economy. The Soviet scientist A.M. Gimani developed a practical method for designing metal shaping machines by use of programming computers. The Soviet scientists Breyelo, Gurfinkel, Kobrinskiy, Syasin, Getlin and Jakobson investigated the problem of muscle currents, which permits the production of protheses steered by current and moved by outside motors enabling the invalid to express only the wish of a particular move, whereby the necessary energy is rendered and conducted by the proper muscles. The Soviet mathematician M.M. Gelfand investigated recently the activity of the heart based on cybernetics. There is 1 figure.

ASSOCIATION: Department of Logical Mathematics, Moscow University im. Lomonosov;  
Academy of Sciences USSR

Card 4/4

MARKOV, Andrey A.

"On Computable invariants"

To be presented at the IMU International Congress of  
Mathematicians 1962 - Stockholm, Sweden, 15-22 Aug 62

Corresponding Member, Acad. of Sci. USSR; Mathematics  
Inst. imeni V. A. Steklov, Acad. of Sci. USSR (1961 position)

ARZUMANYAN, A.A., akademik; BERG, A.I., akademik; ZHUKOV, Ye.M., akademik;  
SEMENOV, N.N., akademik; VINOGRADOV, V.V., akademik; FRANTSEV, Yu.P.;  
SHCHERBAKOV, D.I., akademik; ANISIMOV, I.I.; GATOVSKIY, L.M.;  
IOVCHUK, M.T.; FEDOSEYEV, P.N., akademik; ROMASHKIN, P.S.; KONSTANTINOV,  
F.V.; MITIN, M.B., akademik; YELYUTIN, V.P.; PLOTNIKOV, K.N.;  
PRUDENSKIY, G.A.; YUDIN, P.F., akademik; RYBAKOV, B.A., akademik;  
KONSTANTINOV, B.P., akademik; KHVOSTOV, V.M.; KEDROV, B.M.; MARKOV,  
A.A.; BAISHEV, S.B., akademik; ALEKSEYEV, M.N., prof.; SKAZKIN, S.D.,  
akademik; ALEKSANDROV, A.D.; POSPELOV, P.N., akademik

Discussion of L.F. Il'ichev's report. Vest. AN SSSR 32 no.12:19-50  
D '62. (MIRA 15:12)

1. Chleny-korrespondenty AN SSSR (for Aleksandrov, Frantsev,  
Anisimov, Gatovskiy, Iovchuk, Romashkin, Konstantinov, Yelyutin,  
Plotnikov, Prudenskiy, Khvostov, Kedrov, Markov). 2. AN Kazakhskoy  
SSR (for Baishev).

(Research)

S/582/62/000/008/004/013  
D405/D301AUTHOR: Markov, A. A. (Moscow)

TITLE: On minimal contact-rectifier two-terminal networks for monotonic symmetrical functions

SOURCE: Problemy kibernetiki. no. 8. Moscow, 1962, 117-121

TEXT: The problem of constructing a minimal positive two-terminal network is solved for monotonic symmetrical functions, the solution being feasible in practice for a sufficiently large number of arguments. The two-terminal network which realizes the given monotonic symmetrical function  $s_n^k(x_1, \dots, x_n)$  is equal to unity if and only if not less than  $k$  of its arguments assume the value 1. Theorem: Any positive two-terminal network which realizes the function  $s_n^k$  contains not less than  $k(n - k + 1)$  contacts ( $1 \leq k \leq n$ ). This theorem is proved by utilizing the concepts of "length" and "width" of a two-terminal network, introduced by Moore and Shannon (see reference). The proof is based on 3 lemmas. Lemma 3: The number of

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On minimal contact- ...

contacts in a positive two-terminal network is not less than the product of its length by its width. This lemma was proved by Moore and Shannon for a network without rectifiers; the author shows that the presence of rectifiers does not affect the validity of the lemma. By setting  $k = \lfloor \frac{n+1}{2} \rfloor$ , it is found that the minimal positive two-terminal network for the function  $s_n^{\lfloor \frac{n+1}{2} \rfloor}$  contains  $\frac{n+1}{2} (n+1 - \frac{n+1}{2})$  contacts. Thus, for even  $n$  the minimal positive network for the function  $s_n^{\frac{n}{2}}$  contains  $\frac{n}{2}(\frac{n}{2} + 1)$  contacts and for odd  $n$  it contains  $(\frac{n+1}{2})^2$  contacts (for the function  $s_n^{\frac{n+1}{2}}$ ). There is 1 fi-

SUBMITTED: October 18, 1961

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MARKOV, A.A.

Constructive mathematics. Trudy Mat. inst. 67:8-14 '62.  
(MIRA 16:2)  
(Mathematical analysis)

MARKOV, A.A.

On computable invariants. Dokl. AN SSSR 146 no.5:1017-1020 0 '62.  
(MIRA 15:10)

1. Matematicheskiy institut im. V.A.Steklova AN SSSR. Chlen-  
korrespondent AN SSSR.

(Invariants)

MARKOV, Andrey Andreyevich, prof.

Constructive mathematics. Fiz mat spisanie BAN 6 no. 2:  
129-136 '63.

1. Moskovski durzhaven universitet, rukovoditel na katedrata  
po matematischeska logika.

16.7000

S/038/63/027/001/003/004  
B112/B186

**AUTHOR:** Markov, A. A.

**TITLE:** Certain algorithms connected with systems of words

**PERIODICAL:** Akademiya nauk SSSR. Izvestiya. Seriya matematicheskaya, v. 27, no. 1, 1963, 107-160

**TEXT:** Systems of words in a given alphabet A may be regarded as words in an alphabet obtained from A by adding a new letter which acts as a separation mark (see A.A. Markov, Teoriya algoritmov (Theory of algorithms), Trudy Mat. in-ta im. V. A. Steklova Ak. Nauk SSSR, 42, 1954). In the present paper certain concepts and normal algorithms are considered which are connected with systems of words capable of the above interpretation. The paper has the character of an auxiliary work for further investigations.

√B

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